

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[3]{a^5 b^2} \sqrt{a^6 b^3 c}}{(a^3 b^4) \sqrt[5]{b^5 c^2}}$ .

Answer:  A  $\frac{1}{a^{3/2} b^{29/12}}$      B  $a^{9/5} \sqrt[15]{b^6 c}$      C  $\frac{1}{a^{12/5} b^{39/10} \sqrt{c}}$      D  $\frac{1}{a^{3/2} b^{5/2} \sqrt[20]{c}}$      E  $\frac{a^{5/3} \sqrt[10]{c}}{b^{17/6}}$

→ E

2) Compute all solutions of the system

$$\begin{cases} -2x + 5y + 2 = x + 2y \\ y - 3x = -2x - 2y. \end{cases}$$

Answer:  A  $x = -\frac{2}{3}$  and  $y = -\frac{1}{3}$      B  $x = -\frac{3}{4}$  and  $y = -1$      C  $x = -\frac{6}{5}$  and  $y = \frac{14}{5}$      D  $x = 1$  and  $y = \frac{1}{3}$      E  $x = \frac{2}{5}$  and  $y = -\frac{8}{15}$

→ D

3) Compute all solutions of the inequality  $-|x+1| - x + 1 \leq 2x^2$ .

Answer:  A  $x \leq 0$  or  $x \geq 2$      B  $x \leq -1$  or  $x \geq 0$      C  $x \leq \frac{1}{2}(-3 - \sqrt{5})$  or  $x \geq \frac{1}{2}(1 + \sqrt{13})$      D  $\frac{1}{2}(-1 - \sqrt{5}) \leq x \leq \frac{1}{2}(3 + \sqrt{29})$      E  $x \geq -1$

→ B

4) Compute all solutions of the system of inequalities

$$\begin{cases} x^2 - x - 2 < x^2 \\ x \geq |1 - 2x| + 1. \end{cases}$$

Answer:  A  $\frac{1}{3} \leq x < \frac{2}{3}$      B No  $x$      C  $x > 1$  or  $x \leq 0$      D  $\frac{1}{8}(-3 - \sqrt{41}) < x \leq 0$      E  $\frac{1}{8}(-1 - \sqrt{33}) < x \leq 0$

→ B

5) Find the domain of definition of the expression:  $\log\left(\frac{(1+x)(4+x)}{2+2x}\right)$ .

Answer:  A  $x > -4$      B  $x < \frac{1}{2}$  or  $x > 2$      C  $x < -\frac{3}{2}$  or  $-\frac{1}{4} < x < 1$      D  $x < -3$  or  $-2 < x < 1$      E  $x < -3$  or  $0 < x < 1$

→ A

6) Find all  $x$  such that  $\frac{-1 - 2x}{(4+x)(1+3x)} > 0$ .

Answer:  A  $-2 < x < 0$  or  $x > \frac{3}{2}$      B  $x < \frac{1}{2}$      C  $-\frac{3}{2} < x < \frac{1}{3}$  or  $x > \frac{4}{3}$      D  $\frac{1}{3} < x < 3$      E  $x < -4$  or  $-\frac{1}{2} < x < -\frac{1}{3}$

→ E

7) Compute the limit  $\lim_{x \rightarrow +\infty} e^x - \frac{e^{2x}}{x}$ .

Answer:  A  $-\infty$      B 2     C -1     D -e     E 1     F Does not exist

→ A

8) Compute the limit  $\lim_{x \rightarrow 0^-} \frac{e^{2/x}(1-x)}{3x+2}$ .

Answer:  A -1     B 1     C  $-\pi$      D e     E Does not exist     F 0

→ F

9) Compute the limit  $\lim_{x \rightarrow +\infty} -\frac{1}{x^4} - x - \log(x)$ .

Answer:  A  $-\pi$      B  $-\infty$      C -e     D Does not exist     E 2     F 0

→ B

10) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{-4x^3 + 3x^2 + 1}{-2x^3 + x^2 + 1}$ .

Answer:  A Does not exist     B  $\frac{1}{2}$      C  $+\infty$      D 2     E -1     F  $\frac{3}{2}$

→ D

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**2**

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[3]{a^3b^3}\sqrt[4]{a^6b^2c}}{(a^3b^3)\sqrt[3]{bc^4}}$ .

- Answer:  A  $\frac{1}{a^2b^{5/4}}$      B  $\frac{a^{2/3} \sqrt[10]{c}}{b^{8/3}}$      C  $\frac{1}{\sqrt{ab^{11/6}c^{13/12}}}$      D  $\frac{a^{11/3}}{bc^{4/3}}$      E  $\frac{\sqrt{a}}{b^{7/10}c^{3/10}}$

→ **C**

2) Compute all solutions of the system

$$\begin{cases} -5x + 5y + 2 = 2y - 2x \\ x + y = 4x - y. \end{cases}$$

- Answer:  A  $x = -\frac{4}{3}$  and  $y = -2$      B  $x = -3$  and  $y = -7$      C  $x = \frac{2}{11}$  and  $y = \frac{8}{33}$      D  $x = -\frac{1}{6}$  and  $y = \frac{1}{2}$   
 E  $x = -\frac{2}{7}$  and  $y = \frac{8}{7}$

→ **A**

3) Compute all solutions of the inequality  $3x^2 < 1 - x + |x + 3|$ .

- Answer:  A  $-1 < x < -\frac{1}{2}$  or  $-\frac{1}{2} < x < 1$      B  $-\frac{1}{4} < x < 1$      C  $-\frac{2}{3} < x < 0$      D  $\frac{1}{2}(1 - \sqrt{7}) < x < \frac{1}{2}(1 + \sqrt{7})$   
 E  $-\frac{2}{\sqrt{3}} < x < \frac{2}{\sqrt{3}}$

→ **E**

4) Compute all solutions of the system of inequalities

$$\begin{cases} x - 2 \leq x^2 - x \\ 2x - 3 > |-2x - 1|. \end{cases}$$

- Answer:  A  $-\frac{1}{4} < x \leq \frac{1}{2}(\sqrt{5} - 1)$      B  $x > -\frac{1}{4}$      C  $\sqrt{6} - 2 \leq x < 2$      D  $-\frac{2}{3} < x < 0$      E No  $x$

→ **E**

5) Find the domain of definition of the expression:  $\sqrt{\frac{(2+x)(4+x)}{1+3x}}$ .

- Answer:  A  $-4 \leq x \leq -\frac{1}{2}$  or  $x > 2$      B  $x \leq -2$  or  $1 < x \leq \frac{3}{2}$      C  $-3 \leq x \leq -1$  or  $x > 0$   
 D  $-4 \leq x \leq -2$  or  $x > -\frac{1}{3}$      E  $-4 \leq x < -1$  or  $x \geq \frac{2}{3}$

→ **D**

6) Find all  $x$  such that  $\frac{-3-2x}{(3+3x)(-1+3x)} \leq 0$ .

- Answer:  A  $x < -\frac{4}{3}$  or  $\frac{1}{3} < x \leq \frac{3}{2}$      B  $x \leq -3$  or  $-\frac{1}{3} < x < 4$      C  $-3 \leq x < 0$  or  $x > 5$   
 D  $x < -5$  or  $\frac{1}{3} < x \leq 3$      E  $-\frac{3}{2} \leq x < -1$  or  $x > \frac{1}{3}$

→ **E**

7) Compute the limit  $\lim_{x \rightarrow -\infty} e^{-x} - e^{3x}x^2$ .

- Answer:  A 2     B  $+\infty$      C  $-\pi$      D Does not exist     E  $e$      F  $-e$

→ **B**

8) Compute the limit  $\lim_{x \rightarrow 0^-} \frac{e^{-2/x}}{x^2 + x + 1}$ .

- Answer:  A 1     B Does not exist     C  $\pi$      D  $+\infty$      E 2     F  $e$

→ **D**

9) Compute the limit  $\lim_{x \rightarrow 0^+} 3x - \frac{1}{x} - \log(x)$ .

- Answer:  A 1     B  $\pi$      C  $-e$      D Does not exist     E  $-1$      F  $-\infty$

→ **F**

10) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{2x^2 - x + 1}{x^2 - 4x^3}$ .

- Answer:  A  $-\infty$      B  $-\frac{3}{2}$      C  $\frac{1}{2}$      D 1     E Does not exist     F 0

→ **F**

BONUS

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1) Simplify the following expression:  $\frac{(a^3b^4)\sqrt[6]{a^6b^3c^2}}{(a^3b^2)\sqrt[4]{b^5c^6}}$ .

Answer:  A  $\frac{a^4}{c^{3/4}}\sqrt[4]{b}$

B  $\frac{a^4}{b^{11/6}}$

C  $\frac{a^4}{b^{19/12}\sqrt{c}}$

D  $\frac{\sqrt{c}}{a^{2/5}b^{7/4}}$

E  $\frac{ab^{5/4}}{c^{7/6}}$

→ **E**

2) Compute all solutions of the system

$$\begin{cases} -2x - y + 2 = x + 2y \\ -3x - 2y = x + y. \end{cases}$$

Answer:  A  $x = -2$  and  $y = \frac{8}{3}$      B  $x = -\frac{1}{3}$  and  $y = -\frac{1}{2}$      C  $x = \frac{1}{24}$  and  $y = -\frac{7}{24}$      D  $x = \frac{1}{7}$  and  $y = \frac{1}{2}$   
 E  $y = \frac{x}{2} + \frac{1}{3}$

→ **A**

3) Compute all solutions of the inequality  $2x^2 < 1 - x + |2x + 2|$ .

Answer:  A  $-2 < x < -1$  or  $-1 < x < 2$      B  $\frac{1}{4}(1 - \sqrt{17}) < x < \frac{1}{4}(1 + \sqrt{17})$      C  $-1 < x < \frac{3}{2}$   
 D  $\frac{1}{8}(-3 - \sqrt{57}) < x < \frac{1}{8}(1 + \sqrt{17})$      E  $-1 - \sqrt{3} < x < \sqrt{3} - 1$

→ **C**

4) Compute all solutions of the system of inequalities

$$\begin{cases} -x - 2 \leq x^2 + 3x \\ 2x + 1 > |x - 1|. \end{cases}$$

Answer:  A  $\sqrt{3} - 1 \leq x < 1$      B  $x \geq 1 + \sqrt{3}$      C  $-\frac{1}{2} < x \leq 1$      D  $x > 0$      E  $1 - \sqrt{2} \leq x \leq 1 + \sqrt{2}$

→ **D**

5) Find the domain of definition of the expression:  $\sqrt{\frac{(2+x)(3-3x)}{-2-x}}$ .

Answer:  A  $x \geq 1$      B  $-\frac{1}{3} \leq x < 1$  or  $x \geq 2$      C  $-4 \leq x \leq -1$  or  $x > 2$      D  $-1 < x \leq \frac{1}{3}$  or  $x \geq \frac{2}{3}$      E  $x \leq \frac{1}{2}$

→ **A**

6) Find all  $x$  such that  $\frac{1-x}{(4+x)(-2+3x)} > 0$ .

Answer:  A  $x < \frac{1}{3}$  or  $x > \frac{2}{3}$      B  $-\frac{3}{2} < x < 0$  or  $x > 4$      C  $x < -4$  or  $0 < x < \frac{3}{2}$      D  $x < -3$  or  $\frac{2}{3} < x < 2$   
 E  $x < -4$  or  $\frac{2}{3} < x < 1$

→ **E**

7) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{e^{-3x}}{x^2} - e^{2x}x$ .

Answer:  A 1     B  $\pi$      C -1     D 2     E  $-\infty$      F Does not exist

→ **E**

8) Compute the limit  $\lim_{x \rightarrow 0^-} \frac{e^{2/x}(2x+1)}{-x-1}$ .

Answer:  A -1     B  $e$      C 0     D Does not exist     E  $-\pi$      F 2

→ **C**

9) Compute the limit  $\lim_{x \rightarrow 0^+} \frac{3}{x^4} + x - \log(x)$ .

Answer:  A  $-\pi$      B Does not exist     C  $+\infty$      D 2     E  $-\infty$      F  $-e$

→ **C**

10) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{4x^3 + 3x^2 + x + 1}{x^2 - 4x^3}$ .

Answer:  A Does not exist     B -1     C  $-\frac{1}{2}$      D  $-\pi$      E 0     F -3

→ **B**

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1) Simplify the following expression:  $\frac{\sqrt[5]{a^7b^3}\sqrt{a^6b^4c^3}}{(a^2b^4)\sqrt[4]{b^5c^2}}$ .

Answer:  A  $\frac{a^{12/5}c}{b^{53/20}}$

B  $\frac{\sqrt[15]{b}}{a^{7/6}\sqrt[20]{c}}$

C  $\frac{a^{2/3}\sqrt[10]{c}}{b^{8/3}}$

D  $\frac{1}{\sqrt{ab^{107/30}c^{3/2}}}$

E  $\frac{a^4}{b^{8/3}c}$

→ **A**

2) Compute all solutions of the system

$$\begin{cases} 4x + 5y + 2 = 2y - 2x \\ x + y = 4x - 2y. \end{cases}$$

Answer:  A  $x = -\frac{2}{11}$  and  $y = -\frac{8}{11}$     B  $x = -\frac{2}{9}$  and  $y = -\frac{2}{9}$     C  $x = 2$  and  $y = 1$     D  $x = \frac{2}{15}$  and  $y = \frac{7}{15}$     E  $x = \frac{1}{13}$  and  $y = \frac{4}{13}$

→ **B**

3) Compute all solutions of the inequality  $-3|x - 3| + x - 3 \leq -x^2$ .

Answer:  A  $-2 \leq x \leq 2$     B  $x \geq -9$     C  $x \leq \frac{1}{2}(-3 - \sqrt{13})$  or  $x \geq \frac{1}{2}(\sqrt{13} - 3)$     D  $-6 \leq x \leq 2$     E  $x \leq -1$

→ **D**

4) Compute all solutions of the system of inequalities

$$\begin{cases} |x - 1| > 2x - 2 \\ 2x > -3x^2 - 2x + 2. \end{cases}$$

Answer:  A  $x < -\frac{1}{3}$  or  $0 < x < 3$     B  $x < -\frac{1}{3}$  or  $0 < x < \frac{2}{3}$     C  $-1 < x < 0$  or  $x > 0$     D  $x < \frac{1}{3}(-2 - \sqrt{10})$  or  $\frac{1}{3}(\sqrt{10} - 2) < x < 1$     E  $2 - \sqrt{3} < x < 2$

→ **D**

5) Find the domain of definition of the expression:  $\log(-4x^2 + 3x - 3)$ .

Answer:  A No x    B  $\frac{1}{8}(1 - \sqrt{17}) < x < \frac{1}{8}(1 + \sqrt{17})$     C  $x < -1$  or  $x > -\frac{1}{3}$     D  $x > \frac{1}{2}$     E  $-\frac{3}{2} < x < 0$

→ **A**

6) Find all  $x$  such that  $\frac{-3+x}{(4-x)(-2+3x)} > 0$ .

Answer:  A  $x < \frac{2}{3}$  or  $3 < x < 4$     B  $x < -3$  or  $-\frac{1}{2} < x < 0$     C  $x < -\frac{2}{3}$  or  $x > 1$     D  $\frac{1}{3} < x < 1$  or  $x > 2$     E  $-4 < x < -\frac{3}{2}$  or  $x > -\frac{2}{3}$

→ **A**

7) Compute the limit  $\lim_{x \rightarrow +\infty} e^{3x} - e^{2x}x^3$ .

Answer:  A  $+\infty$     B  $-e$     C 1    D  $-\pi$     E Does not exist    F 0

→ **A**

8) Compute the limit  $\lim_{x \rightarrow \frac{1}{3}-} \frac{e^{3/x}}{1 - 3x}$ .

Answer:  A  $-1$     B  $-\infty$     C  $\pi$     D  $-\pi$     E  $+\infty$     F Does not exist

→ **E**

9) Compute the limit  $\lim_{x \rightarrow +\infty} x - \frac{1}{x} + \log(x)$ .

Answer:  A  $+\infty$     B  $-1$     C  $\pi$     D  $-\infty$     E 2    F Does not exist

→ **A**

10) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{3x^2 + 1}{x^2 - 4x^3}$ .

Answer:  A 0    B 1    C Does not exist    D 2    E  $-e$     F  $-\pi$

→ **A**

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1) Simplify the following expression:  $\frac{(a^7b^4)\sqrt[4]{a^6b^3c}}{(a^3b^4)\sqrt[3]{b^5c^6}}$ .

- Answer:  A  $\frac{a^{11/2}}{b^{11/12}c^{7/4}}$      B  $\frac{b^{31/20}\sqrt[10]{c}}{\sqrt{a}}$      C  $\frac{a^{5/3}b^{4/3}}{c^{7/15}}$      D  $\frac{\sqrt{c}}{a^{12/5}b^{59/20}}$      E  $\frac{a^{2/3}}{b^{13/12}\sqrt[3]{c}}$

→ A

2) Compute all solutions of the system

$$\begin{cases} x + 2y + 2 = y - 2x \\ y - 3x = x - 2y. \end{cases}$$

- Answer:  A  $x = -\frac{6}{13}$  and  $y = -\frac{8}{13}$      B  $x = \frac{3}{11}$  and  $y = -\frac{4}{11}$      C  $x = \frac{4}{5}$  and  $y = -\frac{2}{5}$      D  $x = \frac{1}{3}$  and  $y = -1$      E  $x = \frac{3}{10}$  and  $y = \frac{2}{5}$

→ A

3) Compute all solutions of the inequality  $-3|x - 3| - x - 3 \leq 2x^2$ .

- Answer:  A All  $\mathbf{R}$      B  $x \leq -\frac{7}{2}$  or  $x \geq 1$      C  $x \geq \frac{1}{2}$      D  $x \leq -1$  or  $x \geq 1$      E  $\frac{1}{2}(3 - \sqrt{5}) \leq x \leq \frac{1}{2}(3 + \sqrt{5})$

→ A

4) Compute all solutions of the system of inequalities

$$\begin{cases} x + 2 \leq x^2 + 3x \\ 2x - 3 > |x + 1|. \end{cases}$$

- Answer:  A  $x > 4$      B  $2 < x \leq 1 + \sqrt{2}$      C  $-\frac{1}{2} < x \leq \frac{1}{2}(\sqrt{5} - 1)$      D  $-\frac{1}{4} < x \leq \frac{1}{2}(1 + \sqrt{5})$      E  $x \geq 1 + \sqrt{3}$

→ A

5) Find the domain of definition of the expression:  $\log\left(\frac{(-3+2x)(3+2x)}{-1+2x}\right)$ .

- Answer:  A  $x < -1$  or  $-1 < x < \frac{1}{4}$      B  $-\frac{3}{2} < x < \frac{1}{2}$  or  $x > \frac{3}{2}$      C  $-3 < x < 0$  or  $x > \frac{1}{2}$   
 D  $x < 0$  or  $1 < x < 3$      E  $-\frac{1}{4} < x < 0$  or  $x > 2$

→ B

6) Find all  $x$  such that  $\frac{-3+2x}{(3-x)(2+3x)} > 0$ .

- Answer:  A  $x < -\frac{2}{3}$  or  $\frac{3}{2} < x < 3$      B  $x < -\frac{3}{2}$  or  $-\frac{1}{3} < x < 2$      C  $\frac{2}{3} < x < 3$  or  $x > 4$      D  $x < -\frac{1}{3}$  or  $x > 2$   
 E  $\frac{1}{2} < x < \frac{2}{3}$  or  $x > 4$

→ A

7) Compute the limit  $\lim_{x \rightarrow -\infty} e^{2x}x^3 - \frac{e^{3x}}{x^2}$ .

- Answer:  A  $\pi$      B  $-\infty$      C  $+\infty$      D Does not exist     E  $-\pi$      F 0

→ F

8) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{e^{2/x}(2x-2)}{3x+2}$ .

- Answer:  A  $\pi$      B  $-\pi$      C 2     D  $\frac{2}{3}$      E 1     F Does not exist

→ D

9) Compute the limit  $\lim_{x \rightarrow 0+} -x + \frac{1}{x} - 3 \log(x)$ .

- Answer:  A Does not exist     B  $-\pi$      C  $-e$      D 1     E 2     F  $+\infty$

→ F

10) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{-2x^3 + x^2 + 1}{2x^3 + x^2 + 1}$ .

- Answer:  A  $\frac{1}{2}$      B Does not exist     C 3     D -1     E  $-e$      F  $+\infty$

→ D

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1) Simplify the following expression:  $\frac{(a^9b^4)\sqrt[4]{a^4b^4c^2}}{(a^4b^2)\sqrt[5]{b^3c^6}}$ .

Answer:  A  $\frac{\sqrt{c}}{b^{7/4}}$

B  $\frac{\sqrt{a}}{b^{7/10}c^{3/10}}$

C  $\frac{a^{7/15}}{b^{49/15}c^{7/10}}$

D  $\frac{a^6b^{12/5}}{c^{7/10}}$

E  $a^{11/2}\sqrt{b}\sqrt[3]{c}$

→ **D**

2) Compute all solutions of the system

$$\begin{cases} -2x - 4y - 2 = x + 2y \\ x + y = -2x - y. \end{cases}$$

Answer:  A  $x = \frac{1}{3}$  and  $y = \frac{1}{6}$

B  $x = \frac{1}{2}$  and  $y = \frac{7}{2}$

C  $x = \frac{1}{3}$  and  $y = -\frac{1}{2}$

D  $y = \frac{x}{2} - \frac{1}{3}$

E  $x = -2$  and  $y = -1$

→ **C**

3) Compute all solutions of the inequality  $2x^2 + |x - 2| \geq x$ .

Answer:  A  $x \leq -4$  or  $x \geq \frac{4}{3}$   B  $x \geq 4$   C All **R**  D  $\frac{1}{4}(1 - \sqrt{33}) \leq x \leq \frac{1}{4}(1 + \sqrt{33})$   E  $\frac{1}{4}(1 - \sqrt{33}) \leq x \leq \frac{5}{2}$

→ **C**

4) Compute all solutions of the system of inequalities

$$\begin{cases} |x + 1| > 2x + 1 \\ x > -3x^2 - 2x + 2. \end{cases}$$

Answer:  A  $-3 < x < -1$  or  $x > -\frac{1}{3}$

B  $x < \frac{1}{6}(-3 - \sqrt{33})$

C  $x < 0$  or  $0 < x < 3$

D No **x**

E  $x > 1$  or  $x \leq 0$

→ **B**

5) Find the domain of definition of the expression:  $\sqrt{\frac{(1-2x)(3-3x)}{-2-x}}$ .

Answer:  A  $-1 \leq x < \frac{1}{3}$  or  $x \geq \frac{4}{3}$   B  $x \leq -1$   C  $x \leq -2$  or  $-\frac{2}{3} < x \leq \frac{1}{3}$   D  $x \leq -\frac{3}{2}$  or  $1 < x \leq 4$   E  $x < -2$  or  $\frac{1}{2} \leq x \leq 1$

→ **E**

6) Find all  $x$  such that  $\frac{(1+2x)(4+x)}{3x} \geq 0$ .

Answer:  A  $x < -\frac{1}{3}$  or  $\frac{2}{3} \leq x \leq 3$   B  $x < \frac{2}{3}$  or  $\frac{4}{3} \leq x \leq \frac{3}{2}$   C  $-2 \leq x < \frac{1}{3}$   D  $x < 0$  or  $x \geq 1$   E  $-4 \leq x \leq -\frac{1}{2}$  or  $x > 0$

→ **E**

7) Compute the limit  $\lim_{x \rightarrow -\infty} e^{-x}x^2 - \frac{e^{3x}}{x^3}$ .

Answer:  A  $+\infty$

B 2

C -1

D Does not exist

E 0

F 1

→ **A**

8) Compute the limit  $\lim_{x \rightarrow 0^-} \frac{e^{-2/x}(2x-2)}{-x-1}$ .

Answer:  A -1

B  $-\pi$

C  $\pi$

D Does not exist

E  $-\infty$

F  $+\infty$

→ **F**

9) Compute the limit  $\lim_{x \rightarrow 0^+} -x - \frac{3}{x} - \log(x)$ .

Answer:  A  $-\infty$

B Does not exist

C  $e$

D  $+\infty$

E  $\pi$

F -1

→ **A**

10) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{-4x^3 + x^2 - 2x + 1}{x^2 - 4x^3}$ .

Answer:  A Does not exist

B  $\pi$

C 0

D -1

E 1

F  $e$

→ **E**

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[3]{a^7b^4}\sqrt[6]{a^4b^4c^3}}{(a^4b^4)\sqrt[5]{bc^4}}$ .

- Answer:  A  $\frac{3\sqrt{c}}{\sqrt[6]{ab^{19/12}}}$      B  $\frac{a^{7/5}c^{4/3}}{b^{3/2}}$      C  $\frac{1}{ab^{11/5}c^{3/10}}$      D  $\frac{1}{\sqrt[3]{ab^{11/6}c^{3/2}}}$      E  $\frac{c^{3/5}}{\sqrt[6]{ab^{53/30}}}$

→ C

2) Compute all solutions of the system

$$\begin{cases} 4x - 4y - 2 = 2y - 2x \\ x - 2y = 4x - y. \end{cases}$$

- Answer:  A  $x = \frac{2}{15}$  and  $y = \frac{2}{5}$      B  $x = -\frac{3}{5}$  and  $y = -\frac{4}{5}$      C  $x = \frac{1}{12}$  and  $y = -\frac{1}{4}$      D  $x = \frac{6}{5}$  and  $y = \frac{2}{5}$      E  $x = -\frac{4}{7}$  and  $y = 2$

→ C

3) Compute all solutions of the inequality  $-2x^2 + |x + 2| \geq -x - 4$ .

- Answer:  A  $\frac{1}{2}(1 - \sqrt{13}) \leq x \leq \frac{1}{2}(1 + \sqrt{13})$      B  $x \geq -\frac{4}{5}$      C  $x \leq -4$  or  $x \geq 0$   
 D  $\frac{1}{4}(-3 - \sqrt{41}) \leq x \leq \frac{1}{4}(1 + \sqrt{33})$      E  $\frac{1}{4}(-1 - \sqrt{33}) \leq x \leq \frac{1}{4}(\sqrt{33} - 1)$

→ A

4) Compute all solutions of the system of inequalities

$$\begin{cases} |x + 3| > 2x - 2 \\ 2x > x^2 + x. \end{cases}$$

- Answer:  A  $x < -1$  or  $\frac{2}{3} < x < 1$      B  $-3 < x < \frac{1}{3}(-2 - \sqrt{10})$  or  $x > \frac{1}{3}(\sqrt{10} - 2)$   
 C  $x < -\sqrt{\frac{2}{3}}$  or  $\sqrt{\frac{2}{3}} < x < 1$      D  $\frac{1}{2}(1 - \sqrt{5}) < x < 0$      E  $0 < x < 1$

→ E

5) Find the domain of definition of the expression:  $\log\left(\frac{(-3+x)(2-2x)}{-1-x}\right)$ .

- Answer:  A  $-\frac{1}{2} < x < 2$  or  $x > 3$      B  $x < -1$  or  $0 < x < 4$      C  $x < -2$  or  $-\frac{1}{2} < x < \frac{3}{2}$   
 D  $x < -3$  or  $0 < x < \frac{1}{2}$      E  $-1 < x < 1$  or  $x > 3$

→ E

6) Find all  $x$  such that  $\frac{-1+2x}{(3+x)(-2+3x)} \leq 0$ .

- Answer:  A  $x < -4$  or  $\frac{2}{3} < x \leq 3$      B  $x < -3$  or  $\frac{1}{2} \leq x < \frac{2}{3}$      C  $x < \frac{1}{3}$  or  $1 \leq x < 4$   
 D  $x < -5$  or  $-1 \leq x < \frac{1}{3}$      E  $x < -\frac{2}{3}$  or  $x > 5$

→ B

7) Compute the limit  $\lim_{x \rightarrow -\infty} e^{-2x} - e^{3x}x$ .

- Answer:  A  $+\infty$      B Does not exist     C  $-\pi$      D 0     E  $-e$      F 2

→ A

8) Compute the limit  $\lim_{x \rightarrow 0^+} \frac{e^{-2/x}(2x+1)}{x-1}$ .

- Answer:  A Does not exist     B 2     C  $-e$      D  $-\pi$      E 0     F  $e$

→ E

9) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{5}{x^4} + x - \log(x)$ .

- Answer:  A Does not exist     B 0     C  $-e$      D  $+\infty$      E  $\pi$      F 1

→ D

10) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{-4x^3 + 3x^2 - x + 1}{2x^3 + x^2 + 1}$ .

- Answer:  A Does not exist     B  $+\infty$      C -1     D -2     E  $\frac{3}{2}$      F  $-e$

→ D

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{(a^7b^2)\sqrt[6]{a^6b^4c^2}}{(a^3b^3)\sqrt[4]{b^3c^4}}$ .

- Answer:  A  $\frac{\sqrt[10]{a}}{b^{19/6}c^{3/2}}$      B  $\frac{a^5}{b^{13/12}c^{2/3}}$      C  $\frac{a^{4/3}}{b}$      D  $\frac{a^4\sqrt[4]{b}}{c^{3/4}}$      E  $\frac{a^{20/3}}{b^{5/12}\sqrt[3]{c}}$

→ B

2) Compute all solutions of the system

$$\begin{cases} -5x - 4y - 2 = y - 2x \\ -3x - 2y = 2y - 2x. \end{cases}$$

- Answer:  A  $x = -\frac{1}{12}$  and  $y = \frac{1}{3}$      B  $x = \frac{1}{7}$  and  $y = \frac{4}{7}$      C  $x = -\frac{8}{7}$  and  $y = \frac{2}{7}$      D  $x = \frac{2}{5}$  and  $y = -\frac{4}{5}$      E  $x = -\frac{2}{21}$  and  $y = \frac{1}{3}$

→ C

3) Compute all solutions of the inequality  $-3|x - 1| + x - 1 \leq 2x^2$ .

- Answer:  A All  $\mathbf{R}$      B  $-\sqrt{2} \leq x \leq 3 + \sqrt{5}$      C  $x \leq -1 - \sqrt{2}$  or  $x \geq \sqrt{2} - 1$      D  $-1 - \sqrt{5} \leq x \leq 2 + \sqrt{2}$      E  $\frac{1}{2}(1 - \sqrt{21}) \leq x \leq \frac{1}{2}(5 + \sqrt{29})$

→ A

4) Compute all solutions of the system of inequalities

$$\begin{cases} |3 - x| - 2x \leq -2 \\ x^2 + x + 1 > 1 - 3x. \end{cases}$$

- Answer:  A  $3 \leq x < 4$      B  $x \geq \frac{5}{3}$      C  $-3 < x \leq -\frac{5}{3}$      D  $\frac{2}{3} \leq x < 1$      E No  $x$

→ B

5) Find the domain of definition of the expression:  $\log\left(\frac{(-4+2x)(2-x)}{-1-4x}\right)$ .

- Answer:  A  $x < -\frac{3}{2}$  or  $2 < x < 4$      B  $x < -\frac{1}{2}$  or  $1 < x < 3$      C  $-\frac{1}{4} < x < 2$  or  $x > 2$      D  $x < \frac{1}{2}$  or  $\frac{3}{2} < x < 4$      E  $-1 < x < 2$  or  $x > 4$

→ C

6) Find all  $x$  such that  $\frac{(-1+x)(4-x)}{-1+3x} \geq 0$ .

- Answer:  A  $-1 \leq x < -\frac{1}{3}$  or  $x \geq 3$      B  $x < \frac{1}{3}$  or  $1 \leq x \leq 4$      C e     D  $x \leq -2$  or  $\frac{1}{3} < x \leq \frac{1}{2}$      E  $-2 \leq x < -\frac{1}{3}$  or  $x \geq 3$

→ B

7) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{e^{-3x}}{x} - e^{2x}x$ .

- Answer:  A Does not exist     B  $+\infty$      C  $-\pi$      D 2     E  $\pi$      F  $-\infty$

→ F

8) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{e^{-2/x}(1-x)}{x+2}$ .

- Answer:  A -1     B  $\pi$      C 2     D  $\frac{2}{3}$      E 1     F Does not exist

→ A

9) Compute the limit  $\lim_{x \rightarrow 0+} -\frac{1}{x^4} - x + \log(x)$ .

- Answer:  A -e     B Does not exist     C 0     D  $-\pi$      E  $+\infty$      F  $-\infty$

→ F

10) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{-2x^3 + 3x^2 - 3x + 1}{4x^3 + x^2}$ .

- Answer:  A -e     B Does not exist     C 1     D  $-\frac{1}{2}$      E  $\frac{1}{2}$      F  $-\frac{3}{2}$

→ D

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[5]{a^9 b^2} \sqrt[6]{a^6 b^3 c^4}}{(a^2 b^2) \sqrt[5]{b c^4}}$ .

- Answer:  A  $\frac{1}{a^{3/5} b^{5/4} c^{11/20}}$      B  $\frac{a^{4/3} c}{b^{29/12}}$      C  $\frac{a^{4/5}}{b^{13/10} c^{2/15}}$      D  $\frac{a^9 b^{15/4}}{\sqrt{c}}$      E  $\frac{b^{13/10}}{c^{3/10}}$

→ C

2) Compute all solutions of the system

$$\begin{cases} -5x - y - 2 = x + y \\ x + y = -2x - 2y. \end{cases}$$

- Answer:  A  $x = 0$  and  $y = -\frac{1}{2}$      B  $x = -\frac{6}{5}$  and  $y = \frac{8}{5}$      C  $x = -\frac{4}{13}$  and  $y = \frac{2}{13}$      D  $x = -\frac{1}{3}$  and  $y = -\frac{1}{3}$      E  $x = -\frac{1}{2}$  and  $y = \frac{1}{2}$

→ E

3) Compute all solutions of the inequality  $-2x^2 + |-x - 2| \geq -3x - 2$ .

- Answer:  A  $x \leq \frac{1}{4}(-1 - \sqrt{33})$  or  $x \geq \frac{1}{4}(\sqrt{33} - 1)$      B  $x \leq -\sqrt{2}$  or  $x \geq 1$      C  $1 - \sqrt{3} \leq x \leq 1 + \sqrt{3}$      D  $x \leq 0$  or  $x \geq 4$      E  $x \geq -3$

→ C

4) Compute all solutions of the system of inequalities

$$\begin{cases} |3 - x| + 2x \leq 1 \\ x^2 - 2x + 1 > 1 - 3x. \end{cases}$$

- Answer:  A  $x \leq -2$      B  $x \geq \frac{2}{3}$      C  $2 \leq x < 4$      D  $0 < x < 1$      E  $3 \leq x < 4$

→ A

5) Find the domain of definition of the expression:  $\log\left(\frac{(-3+2x)(3-x)}{2x}\right)$ .

- Answer:  A  $-1 < x < 1$  or  $x > 3$      B  $x < 1$  or  $x > 4$      C  $x < -1$  or  $3 < x < 4$      D  $1 < x < 2$  or  $x > 2$      E  $x < 0$  or  $\frac{3}{2} < x < 3$

→ E

6) Find all  $x$  such that  $\frac{-3+2x}{(2-3x)(3x)} > 0$ .

- Answer:  A  $x < \frac{2}{3}$  or  $3 < x < 4$      B  $-1 < x < -\frac{2}{3}$  or  $x > 1$      C  $-4 < x < 0$  or  $x > 1$      D  $x < -3$  or  $0 < x < \frac{3}{2}$      E  $x < 0$  or  $\frac{2}{3} < x < \frac{3}{2}$

→ E

7) Compute the limit  $\lim_{x \rightarrow +\infty} e^{-2x} - \frac{e^{-x}}{x}$ .

- Answer:  A Does not exist     B  $+\infty$      C  $-1$      D  $\pi$      E  $0$      F  $-\pi$

→ E

8) Compute the limit  $\lim_{x \rightarrow 0^-} \frac{e^{\frac{1}{x}}}{-x^2 + x + 1}$ .

- Answer:  A Does not exist     B  $\pi$      C  $-1$      D  $-e$      E  $0$      F  $2$

→ E

9) Compute the limit  $\lim_{x \rightarrow +\infty} x^2 - 3x + \log(x)$ .

- Answer:  A 1     B Does not exist     C  $\pi$      D  $-1$      E  $-\pi$      F  $+\infty$

→ F

10) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{-4x^3 + x^2 - 2x + 1}{-4x^3 + x^2 + 1}$ .

- Answer:  A  $-2$      B  $-e$      C  $-\frac{1}{2}$      D 1     E  $-\infty$      F Does not exist

→ D

**10**

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[5]{a^9b^4}\sqrt[6]{a^2b^2c^4}}{(a^3b^4)\sqrt[5]{b^5c^4}}$ .

Answer:  A  $\frac{a^{23/3}b^{7/12}}{c^{4/3}}$      B  $\frac{1}{a^{13/15}b^{58/15}c^{2/15}}$      C  $\frac{1}{a^{9/10}b^{19/10}c^{3/2}}$      D  $\frac{1}{a^{8/15}b^{41/12}c^{5/6}}$      E  $\frac{a}{b^{2/3}\sqrt[3]{c}}$

→ **B**

2) Compute all solutions of the system

$$\begin{cases} -5x + 5y - 2 = x + y \\ -3x - 2y = 4x + 2y. \end{cases}$$

Answer:  A  $x = -\frac{2}{13}$  and  $y = \frac{7}{26}$      B  $x = -\frac{2}{7}$  and  $y = -\frac{2}{7}$      C  $x = \frac{1}{5}$  and  $y = -\frac{7}{15}$      D  $y = \frac{1}{3} - \frac{x}{2}$   
 E  $y = \frac{3x}{2} + \frac{1}{2}$

→ **A**

3) Compute all solutions of the inequality  $2|x+1| - 3x - 1 \leq 2x^2$ .

Answer:  A  $\frac{1}{2}(-3 - \sqrt{13}) \leq x \leq \frac{1}{2}(1 + \sqrt{21})$      B  $\frac{1}{2}(-1 - \sqrt{5}) \leq x \leq \frac{1}{2}(3 + \sqrt{29})$      C 1     D  $x \leq -\frac{3}{2}$  or  $x = -1$  or  
 $x \geq \frac{1}{2}$      E  $\frac{1}{2}(5 - \sqrt{37}) \leq x \leq \frac{1}{2}(5 + \sqrt{37})$

→ **D**

4) Compute all solutions of the system of inequalities

$$\begin{cases} |1-x| > -2x-2 \\ x > x^2+x. \end{cases}$$

Answer:  A  $x < -\frac{1}{3}$      B No  $x$      C  $x < 0$      D  $x < -1$  or  $-\frac{1}{3} < x < 1$      E  $-1 < x < -\frac{1}{\sqrt{3}}$  or  $x > \frac{1}{\sqrt{3}}$

→ **B**

5) Find the domain of definition of the expression:  $\log\left(\frac{(1-x)(4+2x)}{-1-x}\right)$ .

Answer:  A  $-2 < x < -1$  or  $x > 1$      B  $-\frac{1}{2} < x < \frac{3}{2}$  or  $x > 4$      C  $x < -4$  or  $-2 < x < 0$   
 D  $-3 < x < 0$  or  $x > 3$      E  $-2 < x < \frac{1}{2}$  or  $x > 3$

→ **A**

6) Find all  $x$  such that  $\frac{(-5-3x)(3-x)}{3x} < 0$ .

Answer:  A  $x < -\frac{5}{3}$  or  $0 < x < 3$      B  $-2 < x < -\frac{2}{3}$  or  $x > -\frac{1}{2}$      C  $x < -1$  or  $\frac{2}{3} < x < 1$      D  $x < \frac{1}{3}$   
 E  $x < -2$  or  $\frac{1}{3} < x < \frac{3}{2}$

→ **A**

7) Compute the limit  $\lim_{x \rightarrow +\infty} e^{3x} - \frac{e^{3x}}{x^2}$ .

Answer:  A 0     B -1     C Does not exist     D  $-\infty$      E  $-e$      F  $+\infty$

→ **F**

8) Compute the limit  $\lim_{x \rightarrow 0^+} e^{-3/x} (2x - x^2)$ .

Answer:  A -1     B  $-\pi$      C 0     D  $+\infty$      E  $e$      F Does not exist

→ **C**

9) Compute the limit  $\lim_{x \rightarrow 0^+} x^2 + 3x - \log(x)$ .

Answer:  A -e     B -1     C  $+\infty$      D Does not exist     E 0     F e

→ **C**

10) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{4x^3 + 2x^2 + 1}{x^2 - 4x^3}$ .

Answer:  A  $\frac{3}{2}$      B  $-\frac{3}{2}$      C  $-\infty$      D Does not exist     E 1     F -1

→ **F**

BONUS

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[5]{a^3b^2}\sqrt[6]{a^6b^3c}}{(a^2b^4)\sqrt[5]{bc^6}}$ .

- Answer:  A  $\frac{1}{a^{2/5}b^{33/10}c^{31/30}}$      B  $\frac{1}{b^{37/12}c^{5/6}}$      C  $\frac{1}{a^{3/2}b^{2/3}c^{7/4}}$      D  $\frac{a^{3/2}}{b^{15/4}\sqrt{c}}$      E  $\frac{1}{b^{23/12}}$

→ A

2) Compute all solutions of the system

$$\begin{cases} 4x + 2y + 2 = y - 2x \\ x + y = 4x - y. \end{cases}$$

- Answer:  A  $x = \frac{6}{53}$  and  $y = -\frac{14}{53}$      B  $x = -2$  and  $y = -\frac{14}{3}$      C  $x = -1$  and  $y = -1$      D  $x = \frac{1}{9}$  and  $y = \frac{1}{3}$      E  $x = -\frac{4}{15}$  and  $y = -\frac{2}{5}$

→ E

3) Compute all solutions of the inequality  $2|x - 1| + x - 1 \leq x^2$ .

- Answer:  A  $x \leq \frac{1}{2}$  or  $x \geq 2$      B  $\frac{1}{2}(-1 - \sqrt{13}) \leq x \leq \frac{1}{2}(\sqrt{13} - 1)$      C  $x \leq 2$      D  $x \leq \frac{1}{2}(-1 - \sqrt{5})$  or  $x \geq \frac{1}{2}(\sqrt{5} - 1)$      E  $1 - \sqrt{5} \leq x \leq 2 + \sqrt{6}$

→ D

4) Compute all solutions of the system of inequalities

$$\begin{cases} |-x - 1| + 2x \leq 1 \\ -x^2 + x + 2 > x + 2. \end{cases}$$

- Answer:  A  $3 \leq x < 4$      B  $x \leq 0$      C No  $x$      D  $x > 0$      E  $\frac{2}{3} \leq x < 1$

→ C

5) Find the domain of definition of the expression:  $\sqrt{\frac{(1+x)(4+x)}{1-x}}$ .

- Answer:  A  $-2 \leq x < -1$  or  $x \geq 2$      B  $-\frac{2}{3} < x \leq 2$  or  $x \geq 4$      C  $x \leq -2$  or  $-1 < x \leq \frac{3}{2}$      D  $x \leq -4$  or  $-1 \leq x < 1$      E  $x < 0$  or  $x = 2$

→ D

6) Find all  $x$  such that  $\frac{(-1+x)(2-3x)}{1+3x} < 0$ .

- Answer:  A  $x < -4$  or  $-\frac{1}{3} < x < \frac{1}{2}$      B  $-4 < x < -\frac{2}{3}$      C  $-\frac{1}{2} < x < \frac{1}{3}$  or  $x > 2$      D  $-\frac{1}{3} < x < \frac{2}{3}$  or  $x > 1$      E  $x < -\frac{1}{3}$  or  $\frac{1}{3} < x < 1$

→ D

7) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{e^{-3x}}{x^2} - e^{2x}x^2$ .

- Answer:  A  $\pi$      B  $-\pi$      C  $+\infty$      D Does not exist     E  $-\infty$      F  $-1$

→ C

8) Compute the limit  $\lim_{x \rightarrow -\frac{1}{5}-} \frac{e^{-3/x}}{-5x-1}$ .

- Answer:  A Does not exist     B 2     C  $-e$      D 0     E  $\pi$      F  $+\infty$

→ F

9) Compute the limit  $\lim_{x \rightarrow +\infty} 5x^2 - x + \log(x)$ .

- Answer:  A  $-1$      B 0     C  $-\pi$      D  $+\infty$      E Does not exist     F  $-\infty$

→ D

10) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{2x^3 + 3x^2 + x + 1}{-4x^3 + x^2 + 1}$ .

- Answer:  A 2     B  $-\frac{1}{2}$      C  $\pi$      D  $-\frac{3}{2}$      E Does not exist     F  $-\infty$

→ B

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[5]{a^5 b^4} \sqrt[4]{a^4 b^2 c^2}}{(a^2 b^3) \sqrt[3]{b^3 c^6}}$ .

Answer:  A  $\frac{c^{3/5}}{\sqrt[6]{ab^{53/30}}}$

B  $\frac{c^{2/3}}{b^{2/3}}$

C  $\frac{a^{2/3} \sqrt[10]{c}}{b^{8/3}}$

D  $\frac{1}{b^{27/10} c^{3/2}}$

E  $\frac{\sqrt[10]{a}}{b^{19/6} c^{3/2}}$

→ **D**

2) Compute all solutions of the system

$$\begin{cases} 4x + 5y - 2 = 2y - 2x \\ -3x - 2y = -2x - y. \end{cases}$$

Answer:  A  $x = -8$  and  $y = 2$      B  $x = -6$  and  $y = 2$      C  $x = -\frac{4}{15}$  and  $y = -\frac{14}{15}$      D  $x = \frac{4}{5}$  and  $y = \frac{2}{5}$   
 E  $x = \frac{2}{3}$  and  $y = -\frac{2}{3}$

→ **E**

3) Compute all solutions of the inequality  $2|x+1| - x - 1 \leq 3x^2$ .

Answer:  A  $-3 \leq x \leq -\frac{1}{3}$      B  $x \leq \frac{1}{6}(1 - \sqrt{37})$  or  $x \geq \frac{1}{6}(1 + \sqrt{37})$      C  $x \geq -\frac{1}{2}$      D  $x \geq 0$      E  $x \leq \frac{1}{6}(1 - \sqrt{13})$  or  $x \geq \frac{1}{6}(1 + \sqrt{13})$

→ **E**

4) Compute all solutions of the system of inequalities

$$\begin{cases} |x+3| + 2x \leq -2 \\ x^2 - 2x + 1 > 1 - 3x. \end{cases}$$

Answer:  A No  $x$      B  $-3 < x \leq -\frac{2}{3}$      C  $x \geq \frac{5}{3}$      D  $-3 < x \leq -\frac{5}{3}$      E  $x \leq -\frac{5}{3}$

→ **E**

5) Find the domain of definition of the expression:  $\sqrt{\frac{(1+x)(4+x)}{1+3x}}$ .

Answer:  A  $-1 \leq x < -\frac{2}{3}$  or  $x \geq 2$      B  $-4 \leq x \leq -1$  or  $x > -\frac{1}{3}$      C  $-2 < x \leq \frac{4}{3}$  or  $x \geq \frac{3}{2}$   
 D  $-2 \leq x \leq -1$  or  $x > 1$      E  $-\frac{1}{2} \leq x < 2$  or  $x \geq 3$

→ **B**

6) Find all  $x$  such that  $\frac{-3-2x}{(2+x)(-2+3x)} > 0$ .

Answer:  A  $x < -4$  or  $-1 < x < -\frac{1}{3}$      B  $-\frac{3}{2} < x < 0$  or  $x > \frac{2}{3}$      C  $x < -2$  or  $-\frac{3}{2} < x < \frac{2}{3}$   
 D  $x < -\frac{1}{2}$  or  $-\frac{1}{3} < x < 4$      E  $x < -\frac{2}{3}$  or  $-\frac{1}{2} < x < \frac{4}{3}$

→ **C**

7) Compute the limit  $\lim_{x \rightarrow +\infty} e^{3x} - e^{-x} x^3$ .

Answer:  A 2     B Does not exist     C  $-\infty$      D  $-e$      E  $+\infty$      F  $-\pi$

→ **E**

8) Compute the limit  $\lim_{x \rightarrow -\frac{3}{5}^+} \frac{e^{3/x}}{-5x-3}$ .

Answer:  A  $e$      B  $-\pi$      C  $-\infty$      D Does not exist     E  $\pi$      F 1

→ **C**

9) Compute the limit  $\lim_{x \rightarrow 0^+} 5x^2 + 3x - \log(x)$ .

Answer:  A 1     B  $-1$      C  $\pi$      D Does not exist     E  $+\infty$      F  $-e$

→ **E**

10) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{4x^3 + 2x^2 + x + 1}{2x^3 + x^2 + 1}$ .

Answer:  A  $+\infty$      B 2     C Does not exist     D 3     E  $-\infty$      F  $-1$

→ **B**

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[5]{a^7 b^4} \sqrt[4]{a^4 b^2 c^4}}{(a^2 b^2) \sqrt[3]{b^5 c^6}}$ .

Answer:  A  $\frac{a^{4/3}}{b}$

B  $a^7 c^{4/3}$

C  $\frac{a^{2/5}}{b^{71/30} c}$

D  $\frac{a^{7/2}}{b^{5/4} c^{3/4}}$

E  $\frac{a^{13/2} b^{3/4}}{\sqrt{c}}$

→ **C**

2) Compute all solutions of the system

$$\begin{cases} -5x - y - 2 = 2y - 2x \\ x - 2y = 4x - y. \end{cases}$$

Answer:  A  $x = -\frac{4}{9}$  and  $y = -\frac{14}{9}$

E  $x = \frac{2}{11}$  and  $y = -\frac{14}{33}$

B  $x = -\frac{4}{21}$  and  $y = \frac{2}{7}$

C  $x = \frac{2}{3}$

D  $x = \frac{1}{3}$  and  $y = -1$

→ **D**

3) Compute all solutions of the inequality  $2|x+1| - x - 3 \leq -x^2$ .

Answer:  A 2

E  $\frac{1}{2}(3 - \sqrt{29}) \leq x \leq \frac{1}{2}(\sqrt{5} - 1)$

B  $x \leq -\frac{1}{2}$  or  $x \geq 1$

C  $x \leq 1 - \sqrt{3}$  or  $x \geq 1 + \sqrt{3}$

D  $\frac{1}{2}(5 - \sqrt{29}) \leq x \leq \frac{1}{2}(5 + \sqrt{29})$

→ **E**

4) Compute all solutions of the system of inequalities

$$\begin{cases} |-x - 1| > 2x - 2 \\ 2x > x^2 + x - 2. \end{cases}$$

Answer:  A  $-1 < x < 2$

B  $\frac{1}{2}(3 - \sqrt{17}) < x < 3$

C  $x < -\frac{1}{\sqrt{3}}$  or  $\frac{1}{\sqrt{3}} < x < 2$

D  $x < -\frac{1}{3}$  or  $0 < x < \frac{2}{3}$

E  $-5 < x < 0$  or  $x > 0$

→ **A**

5) Find the domain of definition of the expression:  $\sqrt{\frac{(2+2x)(4-3x)}{1-x}}$ .

Answer:  A  $x < -2$  or  $\frac{2}{3} \leq x \leq \frac{3}{2}$

D  $-1 \leq x < 1$  or  $x \geq \frac{4}{3}$

B  $x < 0$  or  $\frac{4}{3} \leq x \leq 2$

E  $x \leq -4$  or  $-1 \leq x < 0$

C  $-1 \leq x < -\frac{2}{3}$  or  $x \geq 2$

→ **D**

6) Find all  $x$  such that  $\frac{(-1-x)(4-3x)}{1+3x} \geq 0$ .

Answer:  A  $x \leq -\frac{3}{2}$  or  $-\frac{2}{3} < x \leq \frac{4}{3}$

D  $-\frac{1}{3} < x \leq \frac{4}{3}$  or  $x \geq 3$

B  $-1 \leq x < -\frac{1}{3}$  or  $x \geq \frac{4}{3}$

E  $x \leq 1$

C  $x \leq -\frac{3}{2}$  or  $\frac{1}{3} < x \leq 3$

→ **B**

7) Compute the limit  $\lim_{x \rightarrow -\infty} e^x - e^{2x} x$ .

Answer:  A  $-\pi$

B  $+\infty$

C Does not exist

D  $\pi$

E  $e$

F 0

→ **F**

8) Compute the limit  $\lim_{x \rightarrow 0+} \frac{e^{2/x}(2x-2)}{2-x}$ .

Answer:  A  $+\infty$

B  $e$

C  $-\infty$

D Does not exist

E  $-\pi$

F 0

→ **C**

9) Compute the limit  $\lim_{x \rightarrow 0+} -x + \frac{5}{x} - \log(x)$ .

Answer:  A  $\pi$

B 2

C  $-\infty$

D  $+\infty$

E  $-1$

F Does not exist

→ **D**

10) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{2x^3 + 2x^2 - x + 1}{4x^3 + x^2}$ .

Answer:  A 1

B 0

C Does not exist

D  $-3$

E  $-\infty$

F  $\frac{1}{2}$

→ **F**

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{(a^5b^3)\sqrt[6]{a^6b^4c^3}}{(a^2b^4)\sqrt[4]{b^5c^4}}$ .

- Answer:  A  $\frac{a^4}{b^{19/12}\sqrt{c}}$      B  $\frac{1}{a^{11/10}b^{37/10}c^{3/10}}$      C  $\frac{\sqrt[12]{c}}{b}$      D  $\frac{1}{b^{23/12}}$      E  $\frac{\sqrt{c}}{b^{5/ab^{9/20}}}$

→ A

2) Compute all solutions of the system

$$\begin{cases} x + 5y + 2 = y - 2x \\ x - 2y = 2y - 2x. \end{cases}$$

- Answer:  A  $x = \frac{6}{25}$  and  $y = \frac{14}{25}$      B  $y = -2x - \frac{2}{3}$      C  $x = \frac{2}{3}$  and  $y = 1$      D  $x = -\frac{1}{3}$  and  $y = \frac{1}{9}$      E  $x = -\frac{1}{3}$  and  $y = -\frac{1}{4}$

→ E

3) Compute all solutions of the inequality  $-3|x - 3| + x - 1 \leq x^2$ .

- Answer:  A  $-1$      B  $x \geq -3$      C All  $\mathbf{R}$      D  $x \leq -2 - \sqrt{6}$  or  $x \geq \sqrt{6} - 2$      E  $x \leq -1 - \sqrt{3}$  or  $x \geq \sqrt{3} - 1$

→ C

4) Compute all solutions of the system of inequalities

$$\begin{cases} x - 2 \leq 3x - 2x^2 \\ 2x + 1 > |-2x - 1|. \end{cases}$$

- Answer:  A  $0 < x \leq \frac{1}{2}(\sqrt{5} - 1)$      B  $\sqrt{3} - 1 \leq x < 2$      C No  $x$      D  $0 < x < 2$      E  $\frac{1}{2}(1 - \sqrt{5}) \leq x < 0$

→ C

5) Find the domain of definition of the expression:  $\log\left(\frac{(-2+2x)(2+x)}{-2+2x}\right)$ .

- Answer:  A  $x > -2$      B  $0 < x < \frac{3}{2}$  or  $x > 2$      C  $x < -4$  or  $\frac{1}{2} < x < 3$      D  $x < -4$  or  $-2 < x < \frac{3}{2}$      E  $-4 < x < -3$  or  $x > 1$

→ A

6) Find all  $x$  such that  $\frac{(-3+2x)(3-x)}{1+3x} < 0$ .

- Answer:  A  $-\frac{1}{3} < x < \frac{3}{2}$  or  $x > 3$      B  $\frac{1}{3} < x < 4$      C  $x < -2$  or  $-\frac{2}{3} < x < 3$      D  $-3 < x < -\frac{2}{3}$  or  $x > 1$      E  $x > 1$

→ A

7) Compute the limit  $\lim_{x \rightarrow -\infty} e^{-x} - \frac{e^{3x}}{x^2}$ .

- Answer:  A  $+\infty$      B  $\pi$      C  $-1$      D  $-\pi$      E Does not exist     F  $-e$

→ A

8) Compute the limit  $\lim_{x \rightarrow -1+} \frac{e^{5/x}}{-3x - 3}$ .

- Answer:  A  $1$      B  $+\infty$      C  $0$      D  $-1$      E  $-\infty$      F Does not exist

→ E

9) Compute the limit  $\lim_{x \rightarrow 0+} 3x - \frac{3}{x} - 3 \log(x)$ .

- Answer:  A  $\pi$      B  $0$      C  $-\infty$      D  $1$      E  $+\infty$      F Does not exist

→ C

10) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{-4x^3 + x^2 + x + 1}{-2x^3 + x^2 + 1}$ .

- Answer:  A  $0$      B Does not exist     C  $-3$      D  $-\frac{1}{2}$      E  $+\infty$      F  $2$

→ F

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{(a^7b^4)\sqrt[6]{a^6b^2c^4}}{(a^3b^3)\sqrt[3]{b^3c^4}}$ .

- Answer:  A  $\frac{a^{9/2}b^{4/5}}{c^{7/10}}$      B  $\frac{a^{19/3}}{b^{5/2}c^{31/30}}$      C  $\frac{a^{2/3}}{b^{11/30}c^{19/20}}$      D  $\frac{a^5\sqrt[3]{b}}{c^{2/3}}$      E  $\frac{1}{a^{5/6}b^{41/12}}$

→D

2) Compute all solutions of the system

$$\begin{cases} 4x + 5y - 2 = x + 2y \\ x + y = 4x + 2y. \end{cases}$$

- Answer:  A  $x = -\frac{2}{9}$  and  $y = \frac{1}{9}$      B  $x = -\frac{8}{19}$  and  $y = \frac{2}{19}$      C  $x = -\frac{1}{6}$  and  $y = \frac{1}{2}$      D  $x = -\frac{1}{3}$  and  $y = 1$      E  $x = \frac{2}{13}$  and  $y = \frac{14}{13}$

→D

3) Compute all solutions of the inequality  $-3|x - 3| + x - 3 > -x^2$ .

- Answer:  A  $x < \frac{1}{4}(-1 - \sqrt{73})$  or  $x > \frac{1}{4}(\sqrt{73} - 1)$      B  $x < \frac{1}{6}(1 - \sqrt{13})$  or  $x > \frac{1}{6}(1 + \sqrt{13})$      C  $x < -1 - \sqrt{13}$  or  $x > \sqrt{13} - 1$      D  $-2 - \sqrt{6} < x < \sqrt{6} - 2$      E  $x < -6$  or  $x > 2$

→E

4) Compute all solutions of the system of inequalities

$$\begin{cases} 2x^2 + 3x - 2 < -2x^2 \\ -x \geq |2x - 1| + 1. \end{cases}$$

- Answer:  A  $-1 \leq x \leq -\frac{1}{3}$      B  $\frac{1}{3} \leq x < \frac{1}{2}(\sqrt{17} - 3)$      C No  $x$      D  $x > 1$  or  $x \leq 0$      E  $\frac{1}{3} \leq x \leq 1$

→C

5) Find the domain of definition of the expression:  $\sqrt{\frac{(1-3x)(2-3x)}{-2-x}}$ .

- Answer:  A  $\frac{1}{3} < x \leq 3$      B  $x < \frac{2}{3}$  or  $x \geq 3$      C  $-2 \leq x < -1$  or  $x \geq \frac{1}{3}$      D  $x \leq -3$  or  $-1 < x \leq -\frac{1}{2}$      E  $x < -2$  or  $\frac{1}{3} \leq x \leq \frac{2}{3}$

→E

6) Find all  $x$  such that  $\frac{3+2x}{(5+x)(-2+3x)} \leq 0$ .

- Answer:  A  $x < -1$  or  $-\frac{2}{3} < x \leq 1$      B  $-3 < x < 0$  or  $x \geq 3$      C  $x < -5$  or  $-\frac{3}{2} \leq x < \frac{2}{3}$      D  $x < -5$  or  $-\frac{2}{3} < x \leq 1$      E  $-\frac{4}{3} < x < 0$

→C

7) Compute the limit  $\lim_{x \rightarrow -\infty} e^{-2x}x^3 - e^x x^2$ .

- Answer:  A 2     B Does not exist     C  $-e$      D  $-\infty$      E  $+\infty$      F  $\pi$

→D

8) Compute the limit  $\lim_{x \rightarrow 0^-} \frac{e^{2/x}(-x-2)}{2-x}$ .

- Answer:  A 1     B  $-e$      C  $e$      D Does not exist     E  $-1$      F 0

→F

9) Compute the limit  $\lim_{x \rightarrow +\infty} x - \frac{3}{x} + \log(x)$ .

- Answer:  A 0     B 2     C  $-\infty$      D  $+\infty$      E Does not exist     F  $-\pi$

→D

10) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{-6x^3 + 2x^2 + x + 1}{2x^3 + x^2 + 1}$ .

- Answer:  A  $\frac{1}{2}$      B  $-\frac{1}{2}$      C  $-3$      D Does not exist     E  $+\infty$      F  $-2$

→C

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[5]{a^7b^4}\sqrt[6]{a^4b^4c^3}}{(a^3b^2)\sqrt[4]{b^3c^6}}.$

- Answer:  A  $\frac{1}{a^{3/2}b^{29/12}}$      B  $\frac{1}{\sqrt[3]{ab}\sqrt[3]{c}}$      C  $\frac{1}{a^{14/15}b^{77/60}c}$      D  $\frac{a}{b^{37/20}}$      E  $\frac{1}{a^{3/2}b^{2/3}c^{7/4}}$

→ C

2) Compute all solutions of the system

$$\begin{cases} -5x - y - 2 = 2y - 2x \\ x - 2y = -2x - y. \end{cases}$$

- Answer:  A  $x = -\frac{1}{6}$  and  $y = -\frac{1}{2}$      B  $x = -\frac{6}{5}$  and  $y = \frac{14}{5}$      C  $x = -\frac{4}{21}$  and  $y = \frac{1}{3}$      D  $x = \frac{6}{11}$  and  $y = -\frac{14}{11}$   
 E  $x = -\frac{1}{4}$  and  $y = \frac{7}{12}$

→ A

3) Compute all solutions of the inequality  $2|x - 3| - 3x - 1 > -3x^2$ .

- Answer:  A  $x < \frac{1}{2}(3 - \sqrt{5})$  or  $x > \frac{1}{2}(3 + \sqrt{5})$      B  $x < \frac{1}{2}$      C  $x < \frac{1}{3}(1 - \sqrt{19})$  or  $x > \frac{1}{3}(1 + \sqrt{19})$      D  $-\sqrt{3}$      E All  
**R**

→ E

4) Compute all solutions of the system of inequalities

$$\begin{cases} |x + 1| - 2x \leq -2 \\ -x^2 - 2x + 1 > 1 - 3x. \end{cases}$$

- Answer:  A  $x \leq -2$      B No  $x$      C  $x < -1$      D  $x < 0$      E  $x \geq \frac{5}{3}$

→ B

5) Find the domain of definition of the expression:  $\sqrt{\frac{(2-3x)(3-x)}{x}}.$

- Answer:  A  $-1 < x \leq \frac{3}{2}$  or  $x \geq 4$      B  $x \leq -4$  or  $-1 < x \leq \frac{1}{2}$      C  $x < -2$  or  $-1 \leq x \leq 3$   
 D  $0 < x \leq \frac{2}{3}$  or  $x \geq 3$      E  $-2 < x \leq \frac{4}{3}$  or  $x \geq 2$

→ D

6) Find all  $x$  such that  $\frac{(1-x)(3-3x)}{2+3x} \geq 0$ .

- Answer:  A  $-\frac{1}{2} \leq x < -\frac{1}{3}$  or  $x \geq 4$      B  $x > -\frac{2}{3}$      C  $x \leq -4$  or  $0 < x \leq 1$      D  $-4 \leq x < \frac{1}{3}$  or  $x \geq \frac{3}{2}$   
 E  $x \leq -4$  or  $-\frac{1}{3} < x \leq \frac{1}{2}$

→ B

7) Compute the limit  $\lim_{x \rightarrow +\infty} e^{-3x} - \frac{e^x}{x^3}$ .

- Answer:  A  $-\infty$      B  $-1$      C Does not exist     D 1     E  $\pi$      F 0

→ A

8) Compute the limit  $\lim_{x \rightarrow -1+} \frac{e^{3/x}}{-3x - 3}$ .

- Answer:  A 2     B Does not exist     C -1     D  $\pi$      E 1     F  $-\infty$

→ F

9) Compute the limit  $\lim_{x \rightarrow +\infty} -x^2 + x + \log(x)$ .

- Answer:  A -1     B Does not exist     C  $-\infty$      D  $-\pi$      E 1     F  $+\infty$

→ C

10) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{-4x^3 + 3x^2 - x + 1}{2x^3 + x^2}$ .

- Answer:  A -3     B  $\pi$      C -2     D  $+\infty$      E 1     F Does not exist

→ C

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[3]{a^7b^4}\sqrt[6]{a^6b^3c^2}}{(a^2b^4)\sqrt[5]{b^3c^6}}$ .

- Answer: [A]  $\frac{a}{b^{11/3}c^{3/2}}$     [B]  $\frac{a^6b^{13/4}}{\sqrt{c}}$     [C]  $\frac{a^{4/3}}{b^{83/30}c^{13/15}}$     [D]  $\frac{a^{4/5}}{b^{13/10}c^{2/15}}$     [E]  $a^5b^{19/10}c^{6/5}$

→ C

2) Compute all solutions of the system

$$\begin{cases} x - y + 2 = 2y - 2x \\ x + y = -2x - y. \end{cases}$$

- Answer: [A]  $x = \frac{6}{29}$  and  $y = \frac{8}{29}$     [B]  $x = 0$  and  $y = -1$     [C]  $x = -\frac{2}{3}$  and  $y = \frac{8}{3}$     [D]  $y = -3x - 2$   
 [E]  $x = -\frac{4}{15}$  and  $y = \frac{2}{5}$

→ E

3) Compute all solutions of the inequality  $-2|x - 1| + x + 1 \leq x^2$ .

- Answer: [A]  $x \leq -\frac{3}{2}$  or  $x \geq 1$     [B]  $-1 - \sqrt{5} \leq x \leq 2 + \sqrt{2}$     [C]  $x \leq \frac{1}{2}(3 - \sqrt{5})$  or  $x \geq \frac{1}{2}(\sqrt{13} - 1)$     [D] 0    [E]  $-\sqrt{3}$

→ C

4) Compute all solutions of the system of inequalities

$$\begin{cases} x - 2 \leq -2x^2 - x \\ x - 3 > |-2x - 1|. \end{cases}$$

- Answer: [A] No  $x$     [B]  $\sqrt{6} - 2 \leq x < 2$     [C]  $x > -\frac{1}{4}$     [D]  $1 - \sqrt{2} \leq x < 0$     [E]  $-\frac{1}{3} < x \leq \frac{1}{2}(1 + \sqrt{5})$

→ A

5) Find the domain of definition of the expression:  $\sqrt{\frac{(-1+x)(3+x)}{1+3x}}$ .

- Answer: [A]  $x \leq -3$  or  $-\frac{2}{3} < x \leq \frac{3}{2}$     [B]  $x \leq -2$  or  $x > 2$     [C]  $-3 \leq x < -\frac{1}{3}$  or  $x \geq 1$   
 [D]  $x \leq -4$  or  $1 < x \leq 3$     [E]  $-4 \leq x < -2$  or  $x \geq 3$

→ C

6) Find all  $x$  such that  $\frac{(-1-x)(3-x)}{-1+3x} \geq 0$ .

- Answer: [A]  $-3 \leq x \leq -\frac{3}{2}$  or  $x > \frac{1}{3}$     [B]  $-4 \leq x < -\frac{1}{3}$  or  $x \geq \frac{1}{2}$     [C]  $-1 \leq x < \frac{1}{3}$  or  $x \geq 3$   
 [D]  $-\frac{3}{2} \leq x < -\frac{1}{3}$  or  $x \geq 2$     [E]  $x \leq -\frac{1}{2}$  or  $\frac{1}{3} < x \leq 3$

→ C

7) Compute the limit  $\lim_{x \rightarrow -\infty} e^x - e^x x$ .

- Answer: [A]  $+\infty$     [B] 2    [C]  $\pi$     [D] Does not exist    [E]  $-\pi$     [F] 0

→ F

8) Compute the limit  $\lim_{x \rightarrow 0^-} \frac{e^{2/x}}{-x^2 + x + 2}$ .

- Answer: [A]  $+\infty$     [B]  $e$     [C] Does not exist    [D] 0    [E]  $\pi$     [F] -1

→ D

9) Compute the limit  $\lim_{x \rightarrow 0^+} x + \frac{3}{x} - \log(x)$ .

- Answer: [A] Does not exist    [B] 0    [C]  $-e$     [D]  $\pi$     [E]  $+\infty$     [F]  $e$

→ E

10) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{4x^3 + 2x^2 - x + 1}{x^2}$ .

- Answer: [A]  $\frac{3}{2}$     [B] Does not exist    [C]  $\frac{1}{2}$     [D]  $+\infty$     [E] -1    [F]  $-\frac{1}{2}$

→ D

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[3]{a^3b^4}\sqrt[4]{a^4b^2c^2}}{(a^2b^3)\sqrt[4]{b^3c^2}}$ .

Answer:  A  $\frac{\sqrt{ab}^{3/10}}{c^{11/20}}$

B  $\frac{a^{3/2}}{b^{15/4}\sqrt{c}}$

C  $\frac{\sqrt{c}}{\sqrt[5]{ab^9/20}}$

D  $\frac{1}{a^{12/5}b^{9/4}}$

E  $\frac{1}{b^{23/12}}$

→ **E**

2) Compute all solutions of the system

$$\begin{cases} -5x + 2y - 2 = x + y \\ x + y = 4x - 2y. \end{cases}$$

Answer:  A  $y = -\frac{3x}{2} - 1$

B  $x = -\frac{1}{2}$  and  $y = -2$

C  $x = \frac{2}{7}$  and  $y = -\frac{1}{14}$

D  $x = 6$  and  $y = -2$

E  $x = -\frac{2}{5}$  and  $y = -\frac{2}{5}$

→ **E**

3) Compute all solutions of the inequality  $|x - 3| - x + 1 \leq x^2$ .

Answer:  A  $x \leq -4$  or  $x \geq 0$   B  $x \leq -1 - \sqrt{2}$  or  $x \geq \sqrt{2} - 1$   C  $-1 - \sqrt{13} \leq x \leq \sqrt{13} - 1$   D  $x \leq \frac{1}{6}(-5 - \sqrt{85})$   
 or  $x \geq \frac{1}{6}(\sqrt{85} - 5)$   E  $x \leq -1 - \sqrt{5}$  or  $x \geq \sqrt{5} - 1$

→ **E**

4) Compute all solutions of the system of inequalities

$$\begin{cases} |x + 3| - 2x \leq -2 \\ -x^2 - 2x + 1 > x + 1. \end{cases}$$

Answer:  A No  $x$

B  $x \geq \frac{5}{3}$

C  $-3 < x \leq -2$

D  $0 < x < 4$

E  $-3 < x \leq -1$

→ **A**

5) Find the domain of definition of the expression:  $\sqrt{\frac{(1+2x)(2-x)}{2+3x}}$ .

Answer:  A  $-3 \leq x \leq -\frac{3}{2}$  or  $x > -\frac{2}{3}$

B  $x < -\frac{2}{3}$  or  $-\frac{1}{2} \leq x \leq 2$

C  $x \leq -4$  or  $\frac{1}{3} \leq x < 2$

D  $-\frac{2}{3} < x \leq -\frac{1}{2}$  or  $x \geq 1$

E  $0 < x \leq \frac{4}{3}$

→ **B**

6) Find all  $x$  such that  $\frac{(-1-2x)(3+x)}{2+3x} \geq 0$ .

Answer:  A  $-3 \leq x \leq -\frac{3}{2}$  or  $x > -\frac{2}{3}$

B  $x < -\frac{1}{3}$  or  $\frac{2}{3} \leq x \leq 1$

C  $-4 \leq x \leq -3$  or  $x > 0$

D  $x \leq -\frac{3}{2}$  or  $-\frac{2}{3} < x \leq 1$

E  $x \leq -3$  or  $-\frac{2}{3} < x \leq -\frac{1}{2}$

→ **E**

7) Compute the limit  $\lim_{x \rightarrow +\infty} e^x - \frac{e^{-x}}{x^3}$ .

Answer:  A  $-\pi$

B 2

C 0

D  $+\infty$

E  $\pi$

F Does not exist

→ **D**

8) Compute the limit  $\lim_{x \rightarrow 0+} \frac{e^{\frac{1}{x}}}{-2x^2 + x + 2}$ .

Answer:  A -1

B  $+\infty$

C 2

D Does not exist

E 1

F  $\pi$

→ **B**

9) Compute the limit  $\lim_{x \rightarrow +\infty} -x^2 - 3x + \log(x)$ .

Answer:  A -1

B Does not exist

C  $e$

D  $\pi$

E  $-\infty$

F  $-\pi$

→ **E**

10) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{x^2 - 2x + 1}{-2x^3 + x^2 + 1}$ .

Answer:  A  $+\infty$

B 2

C -3

D Does not exist

E 0

F  $-\frac{3}{2}$

→ **E**

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[5]{a^5b^4}\sqrt[4]{a^4b^2c^2}}{(a^4b^3)\sqrt[3]{b^5c^6}}$ .

- Answer:  A  $\frac{a^{2/3} \sqrt[10]{c}}{b^{8/3}}$      B  $\frac{1}{a^2 b^{10/3} c^{3/2}}$      C  $\frac{a}{\sqrt[12]{bc}}$      D  $\frac{\sqrt[10]{c}}{a^{2/3} b}$      E  $\frac{1}{\sqrt{ab^{11/6} c^{13/12}}}$

→B

2) Compute all solutions of the system

$$\begin{cases} 4x + 5y + 2 = x + 2y \\ x - 2y = 2y - 2x. \end{cases}$$

- Answer:  A  $x = \frac{3}{11}$  and  $y = -\frac{4}{11}$      B  $x = -\frac{8}{5}$  and  $y = \frac{14}{5}$      C  $x = -\frac{8}{21}$  and  $y = -\frac{2}{7}$      D  $x = \frac{2}{15}$  and  $y = \frac{4}{15}$      E  $x = -\frac{2}{27}$  and  $y = \frac{7}{27}$

→C

3) Compute all solutions of the inequality  $2x^2 < 2 - x + |-2x + 1|$ .

- Answer:  A  $-1 < x < 2$      B  $\frac{1}{4}(-3 - \sqrt{33}) < x < 1$      C  $-1 < x < \frac{1}{4}$      D  $-\frac{3}{2} < x < \frac{1}{4}(3 + \sqrt{17})$      E  $-4 < x < 1$

→B

4) Compute all solutions of the system of inequalities

$$\begin{cases} |x - 1| - 2x \leq -2 \\ x^2 + x + 2 > 2 - 3x. \end{cases}$$

- Answer:  A  $x \geq 1$      B  $x \leq -\frac{5}{3}$      C  $-3 < x \leq -\frac{5}{3}$      D  $0 < x < 4$      E  $x \leq -2$

→A

5) Find the domain of definition of the expression:  $\sqrt{\frac{(3-x)(4-x)}{2+x}}$ .

- Answer:  A  $x < -2$  or  $\frac{4}{3} \leq x \leq 2$      B  $-2 < x \leq 3$  or  $x \geq 4$      C  $x \leq -2$  or  $-1 < x \leq \frac{3}{2}$      D  $-\frac{1}{2} \leq x < \frac{1}{3}$  or  $x \geq 2$      E  $-1 < x \leq 3$

→B

6) Find all  $x$  such that  $\frac{3+x}{(3-x)(1+3x)} > 0$ .

- Answer:  A  $-\frac{3}{2} < x < -\frac{2}{3}$  or  $x > 2$      B  $x < -3$  or  $-\frac{3}{2} < x < -\frac{1}{3}$      C  $x < -\frac{1}{3}$  or  $x > 2$      D  $-3 < x < -\frac{3}{2}$  or  $x > 0$      E  $x < -3$  or  $-\frac{1}{3} < x < 3$

→E

7) Compute the limit  $\lim_{x \rightarrow -\infty} e^{-x} - \frac{e^{2x}}{x^3}$ .

- Answer:  A 2     B  $\pi$      C Does not exist     D  $+\infty$      E -1     F 1

→D

8) Compute the limit  $\lim_{x \rightarrow -\frac{3}{5}^+} \frac{e^{\frac{1}{x}}}{-5x - 3}$ .

- Answer:  A -1     B Does not exist     C 2     D  $-\infty$      E -e     F  $+\infty$

→D

9) Compute the limit  $\lim_{x \rightarrow +\infty} x + \frac{1}{x} + \log(x)$ .

- Answer:  A  $-\infty$      B  $-\pi$      C e     D  $+\infty$      E -1     F Does not exist

→D

10) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{-6x^3 + 3x^2 - 2x + 1}{x^2 - 4x^3}$ .

- Answer:  A  $\frac{1}{2}$      B  $\frac{3}{2}$      C  $+\infty$      D Does not exist     E -2     F -3

→B

**20**

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[5]{a^7b^5}\sqrt[4]{a^4b^3c}}{(a^3b^4)\sqrt[3]{bc^4}}$ .

- Answer:  A  $\frac{1}{a^{2/5}b^{43/15}\sqrt[6]{c}}$      B  $\frac{a^6}{\sqrt[8]{b}\sqrt{c}}$      C  $\frac{a^{13/2}b^{3/4}}{\sqrt{c}}$      D  $\frac{a^2c}{b^{31/12}}$      E  $\frac{1}{a^{3/5}b^{31/12}c^{13/12}}$

→ **E**

2) Compute all solutions of the system

$$\begin{cases} -2x - y - 2 = x + y \\ y - 3x = x - y. \end{cases}$$

- Answer:  A  $x = -\frac{1}{10}$  and  $y = \frac{7}{30}$      B  $x = 2$  and  $y = 7$      C  $x = -\frac{4}{47}$  and  $y = -\frac{14}{47}$      D  $x = -\frac{2}{7}$  and  $y = -\frac{4}{7}$   
 E  $x = -\frac{3}{5}$  and  $y = \frac{1}{5}$

→ **D**

3) Compute all solutions of the inequality  $2x^2 + |2x + 2| \geq -x - 2$ .

- Answer:  A  $x \leq \frac{1}{2}(1 - \sqrt{5})$  or  $x \geq \frac{1}{2}(1 + \sqrt{5})$      B  $x \leq \frac{1}{4}(-1 - \sqrt{33})$  or  $x \geq 0$      C  $x \leq \frac{1}{4}(-3 - \sqrt{41})$  or  $x \geq \frac{1}{4}(\sqrt{41} - 3)$      D All **R**     E  $x \leq -\frac{1}{2}$  or  $x \geq \frac{3}{2}$

→ **D**

4) Compute all solutions of the system of inequalities

$$\begin{cases} |1 - x| > 1 - 2x \\ x > x^2 + x. \end{cases}$$

- Answer:  A  $x < -\sqrt{\frac{2}{3}}$  or  $\sqrt{\frac{2}{3}} < x < 1$      B  $0 < x < \sqrt{2}$      C No **x**     D  $2 - \sqrt{3} < x < 1$      E  $-2 < x < 0$  or  $x > 0$

→ **C**

5) Find the domain of definition of the expression:  $\log\left(\frac{(-1+2x)(3+2x)}{-1-x}\right)$ .

- Answer:  A  $-\frac{1}{2} < x < \frac{3}{2}$      B  $-1$      C  $x < -4$  or  $2 < x < 3$      D  $-2 < x < 2$      E  $x < -\frac{3}{2}$  or  $-1 < x < \frac{1}{2}$

→ **E**

6) Find all **x** such that  $\frac{(-1-3x)(2-x)}{-1+3x} < 0$ .

- Answer:  A  $x < -\frac{1}{3}$  or  $\frac{1}{3} < x < 2$      B  $-3 < x < -\frac{1}{2}$  or  $x > \frac{1}{3}$      C  $x < -3$  or  $-\frac{2}{3} < x < \frac{2}{3}$   
 D  $-3 < x < -\frac{3}{2}$  or  $x > \frac{1}{3}$      E  $-3 < x < \frac{1}{2}$  or  $x > \frac{2}{3}$

→ **A**

7) Compute the limit  $\lim_{x \rightarrow -\infty} e^{-x} - e^x x^2$ .

- Answer:  A  $-e$      B Does not exist     C 1     D  $e$      E 0     F  $+\infty$

→ **F**

8) Compute the limit  $\lim_{x \rightarrow 1^+} \frac{e^{-3/x}}{x-1}$ .

- Answer:  A  $-e$      B  $e$      C  $-\infty$      D  $+\infty$      E Does not exist     F  $\pi$

→ **D**

9) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{5}{x^4} - 3x + \log(x)$ .

- Answer:  A  $\pi$      B Does not exist     C  $-\infty$      D  $-e$      E 0     F  $-\pi$

→ **C**

10) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{x^2 + x + 1}{x^2 - 4x^3}$ .

- Answer:  A 3     B Does not exist     C 2     D  $\frac{1}{2}$      E 1     F 0

→ **F**

BONUS

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[5]{a^9 b^5} \sqrt[6]{a^6 b^2 c^2}}{(a^4 b^3) \sqrt[4]{b^3 c^6}}$ .

- Answer:  A  $\frac{c^{3/5}}{a^{3/2} b^{21/20}}$      B  $\frac{1}{a^{6/5} b^{29/12} c^{7/6}}$      C  $\frac{a^6 b^{12/5}}{c^{7/10}}$      D  $\frac{a^{2/3}}{b^{11/30} c^{19/20}}$      E  $\frac{a^{23/3}}{b^{7/4} \sqrt{c}}$

→ **B**

2) Compute all solutions of the system

$$\begin{cases} -2x - y + 2 = x + y \\ y - 3x = 2y - 2x. \end{cases}$$

- Answer:  A  $x = \frac{2}{15}$  and  $y = -\frac{1}{5}$      B  $x = \frac{6}{7}$  and  $y = -\frac{8}{7}$      C  $x = 2$  and  $y = -2$      D  $x = \frac{2}{3}$   
 E  $x = 0$  and  $y = -1$

→ **C**

3) Compute all solutions of the inequality  $2|x+1| - x + 1 > -x^2$ .

- Answer:  A All  $\mathbf{R}$      B  $x < -1$  or  $x > \frac{5}{2}$      C  $x < -1$  or  $x > -\frac{1}{2}$      D  $x < -\sqrt{2}$  or  $x > \frac{1}{2}(\sqrt{5} - 1)$      E  $-2$

→ **A**

4) Compute all solutions of the system of inequalities

$$\begin{cases} x^2 + x + 1 < -2x^2 \\ x \geq |2x + 1| + 1. \end{cases}$$

- Answer:  A  $-2 \leq x < \frac{1}{2}(\sqrt{5} - 3)$      B  $0 \leq x \leq \frac{2}{3}$      C  $0 \leq x < \frac{2}{3}$      D  $\frac{1}{3} \leq x < \frac{1}{6}(\sqrt{33} - 3)$      E No  $x$

→ **E**

5) Find the domain of definition of the expression:  $\sqrt{\frac{(3-3x)(3+x)}{1+x}}$ .

- Answer:  A  $x \leq -3$  or  $-1 < x \leq 1$      B  $-4 \leq x \leq \frac{1}{2}$  or  $x > 1$      C  $-4 \leq x \leq -\frac{3}{2}$  or  $x > -1$      D  $-3 \leq x < -2$   
 E  $x \leq -3$  or  $1 < x \leq \frac{3}{2}$

→ **A**

6) Find all  $x$  such that  $\frac{(-1-x)(3-x)}{2+3x} < 0$ .

- Answer:  A  $-5 < x < -4$  or  $x > \frac{1}{3}$      B  $x < -1$  or  $-\frac{2}{3} < x < 3$      C  $x < -2$  or  $-\frac{1}{3} < x < 3$   
 D  $x < -\frac{5}{3}$  or  $-\frac{2}{3} < x < 3$      E  $-\frac{1}{2} < x < -\frac{1}{3}$  or  $x > \frac{4}{3}$

→ **B**

7) Compute the limit  $\lim_{x \rightarrow +\infty} e^{-2x} - \frac{e^x}{x^3}$ .

- Answer:  A 0     B Does not exist     C  $-\infty$      D  $-\pi$      E  $-e$      F  $e$

→ **C**

8) Compute the limit  $\lim_{x \rightarrow \frac{3}{5}-} \frac{e^{3/x}}{5x-3}$ .

- Answer:  A  $-e$      B  $-\pi$      C Does not exist     D  $-\infty$      E  $-1$      F 1

→ **D**

9) Compute the limit  $\lim_{x \rightarrow 0+} \frac{1}{x^4} - x + \log(x)$ .

- Answer:  A Does not exist     B  $\pi$      C  $e$      D  $+\infty$      E  $-\infty$      F 0

→ **D**

10) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{x^2 + 1}{4x^3 + x^2}$ .

- Answer:  A Does not exist     B 2     C  $-\frac{3}{2}$      D 0     E  $\pi$      F  $+\infty$

→ **D**

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[3]{a^9b^2}\sqrt[4]{a^4b^2c^4}}{(a^3b^3)\sqrt[4]{b^3c^6}}$ .

- Answer:  A  $\frac{1}{a^{3/2}b^{2/3}c^{7/4}}$      B  $\frac{a^7b^{3/4}}{\sqrt{c}}$      C  $\frac{a}{b^{31/12}\sqrt{c}}$      D  $\frac{1}{\sqrt[3]{b}c^{3/20}}$      E  $\frac{a^{4/3}}{b^{8/3}\sqrt{c}}$

→ **C**

2) Compute all solutions of the system

$$\begin{cases} -2x + 5y + 2 = x + y \\ -3x - 2y = 4x + y. \end{cases}$$

- Answer:  A  $x = \frac{6}{37}$  and  $y = -\frac{14}{37}$      B  $x = \frac{2}{3}$  and  $y = \frac{14}{9}$      C  $x = -\frac{2}{3}$  and  $y = -\frac{1}{3}$      D  $x = \frac{8}{3}$  and  $y = -\frac{2}{3}$   
 E  $x = \frac{2}{31}$  and  $y = -\frac{14}{31}$

→ **A**

3) Compute all solutions of the inequality  $2|x+1| - x + 1 \leq 3x^2$ .

- Answer:  A  $x \leq 0$      B  $x \leq -\sqrt{\frac{2}{3}}$  or  $x \geq \sqrt{\frac{2}{3}}$      C  $x \leq \frac{1}{6}(1 - \sqrt{37})$  or  $x \geq \frac{1}{6}(1 + \sqrt{37})$      D  $x \leq -2 - \sqrt{2}$  or  $x \geq 0$   
 E  $x \leq -4$  or  $x \geq \sqrt{3} - 1$

→ **C**

4) Compute all solutions of the system of inequalities

$$\begin{cases} 2x^2 - x - 2 < x^2 \\ x \geq |1 - 2x| - 1. \end{cases}$$

- Answer:  A  $-2 \leq x \leq 0$      B  $\frac{1}{6}(-3 - \sqrt{33}) < x \leq 0$      C  $x > 2$      D  $0 \leq x < 2$      E No  $x$

→ **D**

5) Find the domain of definition of the expression:  $\sqrt{\frac{(2+2x)(3-x)}{-2+x}}$ .

- Answer:  A  $x \leq -3$  or  $0 < x \leq \frac{1}{2}$      B  $x \leq -1$  or  $2 < x \leq 3$      C  $x < 1$  or  $\frac{4}{3} \leq x \leq \frac{3}{2}$      D  $x \geq 0$   
 E  $x \leq -\frac{3}{2}$  or  $-\frac{2}{3} < x \leq 1$

→ **B**

6) Find all  $x$  such that  $\frac{(-5-3x)(3-x)}{3x} < 0$ .

- Answer:  A  $x < -1$  or  $\frac{2}{3} < x < 1$      B  $x < -\frac{5}{3}$  or  $0 < x < 3$      C  $x < -2$  or  $\frac{1}{3} < x < \frac{3}{2}$      D  $x < \frac{1}{3}$   
 E  $-2 < x < -\frac{2}{3}$  or  $x > -\frac{1}{2}$

→ **B**

7) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{e^{-2x}}{x} - e^x x^3$ .

- Answer:  A  $-\infty$      B  $0$      C  $e$      D  $1$      E  $\pi$      F Does not exist

→ **A**

8) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{e^{-2/x}(2x+1)}{-x-1}$ .

- Answer:  A  $\pi$      B  $0$      C Does not exist     D  $1$      E  $-2$      F  $-\pi$

→ **E**

9) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{1}{x^4} + x - \log(x)$ .

- Answer:  A  $-\infty$      B Does not exist     C  $+\infty$      D  $0$      E  $-\pi$      F  $1$

→ **C**

10) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{4x^3 + 2x^2 + x + 1}{-2x^3 + x^2 + 1}$ .

- Answer:  A  $-2$      B  $-\infty$      C Does not exist     D  $-e$      E  $+\infty$      F  $-\frac{1}{2}$

→ **A**

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{(a^3b^4)\sqrt[4]{a^2b^3c^2}}{(a^4b^3)\sqrt[5]{bc^2}}$ .

Answer:  A  $\frac{1}{a^{6/5}b^{29/12}c^{7/6}}$      B  $\frac{a^{5/3}\sqrt[10]{c}}{b^{17/6}}$      C  $\frac{1}{a^{5/3}b^{31/12}c^{7/6}}$      D  $\frac{1}{a^{14/15}b^{77/60}c}$      E  $\frac{b^{31/20}\sqrt[10]{c}}{\sqrt{a}}$

→ E

2) Compute all solutions of the system

$$\begin{cases} 4x - 4y + 2 = x + 2y \\ y - 3x = x - y. \end{cases}$$

Answer:  A  $x = \frac{2}{9}$  and  $y = \frac{4}{9}$      B  $x = -\frac{4}{29}$  and  $y = -\frac{14}{29}$      C  $x = \frac{2}{11}$  and  $y = \frac{14}{11}$      D  $x = -\frac{8}{23}$  and  $y = \frac{2}{23}$      E  $x = \frac{8}{31}$  and  $y = -\frac{14}{31}$

→ A

3) Compute all solutions of the inequality  $-2|x - 3| + x - 1 \leq 3x^2$ .

Answer:  A  $x \leq -1 - \sqrt{2}$  or  $x \geq \sqrt{2} - 1$      B  $-\sqrt{2} \leq x \leq \sqrt{2}$      C  $x \leq \frac{1}{6}(-3 - \sqrt{21})$  or  $x \geq \frac{1}{6}(\sqrt{21} - 3)$      D All  $\mathbf{R}$      E  $x \leq -\frac{3}{2}$  or  $x \geq 1$

→ D

4) Compute all solutions of the system of inequalities

$$\begin{cases} x - 2 \leq -2x^2 - x \\ 2x + 1 > |x + 1|. \end{cases}$$

Answer:  A  $x > 2$      B  $x > 0$      C  $-\frac{1}{4} < x \leq 1 + \sqrt{2}$      D  $x \geq 1 + \sqrt{3}$      E  $0 < x \leq \frac{1}{2}(\sqrt{5} - 1)$

→ E

5) Find the domain of definition of the expression:  $\log\left(\frac{(-3+x)(2+x)}{1-4x}\right)$ .

Answer:  A  $x < -3$  or  $-1 < x < 1$      B  $x < -\frac{1}{2}$  or  $2 < x < 3$      C  $-1 < x < \frac{1}{2}$  or  $x > 2$      D  $-1 < x < \frac{1}{2}$      E  $x < -2$  or  $\frac{1}{4} < x < 3$

→ E

6) Find all  $x$  such that  $\frac{3+2x}{(3+x)(3x)} > 0$ .

Answer:  A  $-2 < x < -\frac{1}{2}$  or  $x > 0$      B  $-3 < x < -\frac{3}{2}$  or  $x > 0$      C  $-4 < x < 0$  or  $x > 1$      D  $-\frac{3}{2} < x < -\frac{1}{3}$  or  $x > 2$      E  $x < -3$  or  $\frac{1}{3} < x < 1$

→ B

7) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{e^{-2x}}{x} - \frac{e^{3x}}{x^2}$ .

Answer:  A  $-1$      B  $2$      C  $-\infty$      D  $+\infty$      E Does not exist     F  $-e$

→ C

8) Compute the limit  $\lim_{x \rightarrow 0^-} e^{-1/x} (-x^2 - x)$ .

Answer:  A  $e$      B  $-1$      C  $0$      D Does not exist     E  $-\pi$      F  $+\infty$

→ F

9) Compute the limit  $\lim_{x \rightarrow +\infty} 3x^2 - 3x + \log(x)$ .

Answer:  A  $-e$      B  $+\infty$      C  $0$      D Does not exist     E  $\pi$      F  $-\infty$

→ B

10) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{2x^3 + x^2 + 1}{x^2 - 4x^3}$ .

Answer:  A  $-\frac{1}{2}$      B  $-1$      C Does not exist     D  $-\pi$      E  $e$      F  $-e$

→ A

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{(a^3b^2)\sqrt[4]{a^2b^4c^4}}{(a^2b^2)\sqrt[5]{b^3c^2}}$ .

- Answer:  A  $a^{3/2}b^{2/5}c^{3/5}$      B  $\frac{c^{5/6}}{\sqrt[3]{ab^{4/3}}}$      C  $\frac{a^{7/3}\sqrt{c}}{b^{43/12}}$      D  $\frac{a^{3/5}c^{7/10}}{b^{9/10}}$      E  $\frac{a^{2/3}}{b^{9/4}c^{2/3}}$

→ **A**

2) Compute all solutions of the system

$$\begin{cases} -5x + 5y + 2 = y - 2x \\ x - 2y = 4x + y. \end{cases}$$

- Answer:  A  $y = -\frac{3x}{2} - \frac{1}{2}$      B  $x = \frac{6}{23}$  and  $y = -\frac{14}{23}$      C  $x = \frac{2}{7}$  and  $y = -\frac{2}{7}$      D  $x = \frac{2}{15}$  and  $y = \frac{1}{5}$   
 E  $x = -\frac{1}{11}$  and  $y = \frac{7}{11}$

→ **C**

3) Compute all solutions of the inequality  $3x^2 < -2 - x + |-x + 2|$ .

- Answer:  A  $-1 < x < 0$      B  $-\frac{2}{3} < x < 0$      C  $0 < x < \frac{1}{3}$      D  $-\sqrt{\frac{5}{2}} < x < \sqrt{\frac{5}{2}}$      E  $-1 - \sqrt{2} < x < \sqrt{2} - 1$

→ **B**

4) Compute all solutions of the system of inequalities

$$\begin{cases} x - 2 \leq x^2 + 3x \\ 2x - 3 > |x + 1|. \end{cases}$$

- Answer:  A  $x \geq 1$      B  $x > 0$      C  $0 < x < 2$      D  $x > 4$      E  $1 - \sqrt{2} \leq x \leq 1 + \sqrt{2}$

→ **D**

5) Find the domain of definition of the expression:  $\sqrt{\frac{(3+2x)(3-3x)}{2-x}}$ .

- Answer:  A  $-4 \leq x < 0$      B  $-\frac{3}{2} \leq x \leq 1$  or  $x > 2$      C  $x \leq -2$  or  $-\frac{1}{3} \leq x < \frac{2}{3}$      D  $-\frac{2}{3} < x \leq \frac{1}{2}$  or  $x \geq 4$   
 E  $x \leq -2$  or  $-\frac{1}{3} < x \leq 2$

→ **B**

6) Find all  $x$  such that  $\frac{(3+x)(4-x)}{1+3x} \geq 0$ .

- Answer:  A  $x \leq -3$  or  $-\frac{1}{3} < x \leq 4$      B  $x \leq -2$  or  $-\frac{1}{2} \leq x < \frac{1}{3}$      C  $\frac{1}{3} < x \leq 1$  or  $x \geq 3$   
 D  $x \leq -\frac{1}{2}$  or  $0 < x \leq \frac{2}{3}$      E  $x < \frac{1}{3}$  or  $\frac{2}{3} \leq x \leq 3$

→ **A**

7) Compute the limit  $\lim_{x \rightarrow +\infty} e^{2x} - \frac{e^{2x}}{x}$ .

- Answer:  A  $-1$      B  $e$      C  $\pi$      D  $+\infty$      E  $-\infty$      F Does not exist

→ **D**

8) Compute the limit  $\lim_{x \rightarrow 0^-} e^{-3/x} (x^2 - x)$ .

- Answer:  A  $\pi$      B  $+\infty$      C  $-e$      D  $-\infty$      E  $-1$      F Does not exist

→ **B**

9) Compute the limit  $\lim_{x \rightarrow 0^+} 3x^2 + x + \log(x)$ .

- Answer:  A  $0$      B  $-\pi$      C Does not exist     D  $1$      E  $+\infty$      F  $-\infty$

→ **F**

10) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{4x^3 + x^2 - x + 1}{-2x^3 + x^2 + 1}$ .

- Answer:  A Does not exist     B  $-\pi$      C  $3$      D  $+\infty$      E  $-2$      F  $0$

→ **E**

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[3]{a^7b^4}\sqrt[4]{a^2b^3c^4}}{(a^3b^2)\sqrt[3]{b^5c^2}}$ .

Answer:  A  $\frac{3\sqrt{c}}{\sqrt[6]{ab^{19/12}}}$

B  $\frac{a^6}{c^{11/6}}$

C  $\frac{a^{11/3}}{b^{29/15}c^{7/10}}$

D  $\frac{1}{a^{2b^{7/5}}c^{13/12}}$

E  $b^{11/4}$

→ **A**

2) Compute all solutions of the system

$$\begin{cases} x - y - 2 = y - 2x \\ -3x - 2y = 4x + 2y. \end{cases}$$

Answer:  A  $x = -\frac{6}{17}$  and  $y = \frac{2}{17}$   B  $x = \frac{4}{7}$  and  $y = -\frac{2}{7}$   C  $x = \frac{4}{13}$  and  $y = -\frac{7}{13}$   D  $x = -\frac{4}{15}$  and  $y = -\frac{2}{15}$   
 E  $x = -\frac{4}{35}$  and  $y = \frac{2}{5}$

→ **C**

3) Compute all solutions of the inequality  $4x^2 < -1 + x + |-x + 1|$ .

Answer:  A  $\frac{1}{2}(3 - \sqrt{5}) < x < \frac{1}{2}(3 + \sqrt{5})$   B No  $x$   C  $\frac{1}{3}(1 - \sqrt{13}) < x < \frac{1}{3}(1 + \sqrt{13})$   
 D  $\frac{1}{8}(-1 - \sqrt{65}) < x < \frac{1}{8}(\sqrt{65} - 1)$   E  $-4 < x < 1$

→ **B**

4) Compute all solutions of the system of inequalities

$$\begin{cases} 2 - x \leq x^2 - x \\ 2x - 3 > |-2x - 1|. \end{cases}$$

Answer:  A  $\sqrt{6} - 2 \leq x < 1$   B  $2 < x \leq 1 + \sqrt{2}$   C No  $x$   D  $x > -\frac{1}{4}$   E  $x \geq 1$

→ **C**

5) Find the domain of definition of the expression:  $\log(-4x^2 + 3x - 3)$ .

Answer:  A  $x > \frac{1}{2}$   B  $-\frac{3}{2} < x < 0$   C  $x < -1$  or  $x > -\frac{1}{3}$   D  $\frac{1}{8}(1 - \sqrt{17}) < x < \frac{1}{8}(1 + \sqrt{17})$   E No  $x$

→ **E**

6) Find all  $x$  such that  $\frac{1+2x}{(2-3x)(2+3x)} > 0$ .

Answer:  A  $x < -4$  or  $-1 < x < \frac{2}{3}$   B  $x < -\frac{2}{3}$  or  $-\frac{1}{2} < x < \frac{2}{3}$   C  $-4 < x < -\frac{3}{2}$  or  $x > \frac{2}{3}$   
 D  $x < -1$  or  $\frac{2}{3} < x < 1$   E  $x < \frac{2}{3}$  or  $x > 1$

→ **B**

7) Compute the limit  $\lim_{x \rightarrow +\infty} e^{-x} - e^{3x}x^3$ .

Answer:  A  $-e$   B  $-1$   C  $-\infty$   D Does not exist  E  $1$   F  $\pi$

→ **C**

8) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{e^{-2/x}(1-x)}{x+2}$ .

Answer:  A Does not exist  B 2  C  $\pi$   D 1  E  $-1$   F  $\frac{2}{3}$

→ **E**

9) Compute the limit  $\lim_{x \rightarrow 0^+} x^2 + 3x - 3\log(x)$ .

Answer:  A  $-e$   B Does not exist  C 1  D  $+\infty$   E 2  F  $-\pi$

→ **D**

10) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{4x^3 + 2x^2 - x + 1}{2x^3 + x^2 + 1}$ .

Answer:  A  $e$   B 2  C Does not exist  D  $-\pi$   E  $-\frac{3}{2}$   F  $-\frac{1}{2}$

→ **B**

Family name:

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For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{(a^7b^2)\sqrt{a^4b^3c}}{(a^4b^3)\sqrt[5]{bc^4}}$ .

Answer:  A  $\frac{a^5b^{3/10}}{c^{3/10}}$

B  $\frac{a^{2/3}c^{8/5}}{b^{13/6}}$

C  $a^5b^{5/4}\sqrt{c}$

D  $\frac{a^{23/3}}{b^{7/4}\sqrt{c}}$

E  $\frac{1}{\sqrt[3]{ab}\sqrt[3]{c}}$

→ **A**

2) Compute all solutions of the system

$$\begin{cases} -5x + 5y + 2 = y - 2x \\ x - 2y = -2x - y. \end{cases}$$

Answer:  A  $x = -\frac{2}{7}$  and  $y = \frac{2}{21}$   B  $x = -\frac{2}{13}$  and  $y = -\frac{14}{39}$   C  $x = -\frac{2}{9}$  and  $y = -\frac{2}{3}$   D  $x = \frac{2}{3}$  and  $y = 1$  → **C**  
 E  $x = \frac{1}{3}$  and  $y = \frac{1}{3}$

3) Compute all solutions of the inequality  $|x - 3| + x - 1 > -2x^2$ .

Answer:  A  $x < 1$  or  $x > 9$   B All **R**  C  $x < -\frac{2}{\sqrt{3}}$  or  $x > \frac{2}{\sqrt{3}}$   D  $x < 1 - \sqrt{3}$  or  $x > 1 + \sqrt{3}$  → **B**  
 E  $\frac{1}{2}(-1 - \sqrt{13}) < x < \frac{1}{2}(\sqrt{13} - 1)$

4) Compute all solutions of the system of inequalities

$$\begin{cases} |x + 3| > 2x + 1 \\ x > -3x^2 - 2x + 2. \end{cases}$$

Answer:  A  $x < \frac{1}{6}(-3 - \sqrt{33})$  or  $\frac{1}{6}(\sqrt{33} - 3) < x < 2$   B  $-2 < x < -1$  or  $x > -\frac{1}{3}$   C  $x < -1$  or  $0 < x < \frac{5}{3}$  → **A**  
 D  $-\frac{5}{3} < x < -1$  or  $x > \frac{2}{3}$   E  $-3 < x < -1$  or  $x > \frac{2}{3}$

5) Find the domain of definition of the expression:  $\sqrt{\frac{(-1 - 2x)(2 + x)}{1 - x}}$ .

Answer:  A  $-2 \leq x \leq -\frac{1}{2}$  or  $x > 1$   B  $-\frac{1}{3} \leq x < 0$  or  $x \geq \frac{2}{3}$   C  $-1 < x \leq 1$  or  $x \geq 2$  → **A**  
 D  $-4 \leq x < -\frac{2}{3}$  or  $x \geq 1$   E  $x < -\frac{1}{3}$  or  $x \geq \frac{2}{3}$

6) Find all  $x$  such that  $\frac{1-x}{(4+x)(-2+3x)} > 0$ .

Answer:  A  $x < -4$  or  $0 < x < \frac{3}{2}$   B  $x < -4$  or  $\frac{2}{3} < x < 1$   C  $x < -3$  or  $\frac{2}{3} < x < 2$  → **B**  
 D  $-\frac{3}{2} < x < 0$  or  $x > 4$   E  $x < \frac{1}{3}$  or  $x > \frac{2}{3}$

7) Compute the limit  $\lim_{x \rightarrow +\infty} e^x - e^{-x}x^2$ .

Answer:  A Does not exist  B  $-\infty$   C  $+\infty$   D 2  E  $-\pi$   F -1 → **C**

8) Compute the limit  $\lim_{x \rightarrow 0^-} \frac{e^{-2/x}}{2x^2 + x + 3}$ .

Answer:  A  $-e$   B  $+\infty$   C  $e$   D 1  E Does not exist  F 0 → **B**

9) Compute the limit  $\lim_{x \rightarrow 0^+} -x + \frac{3}{x} - 3 \log(x)$ .

Answer:  A 2  B Does not exist  C  $-\pi$   D 1  E  $+\infty$   F 0 → **E**

10) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{x^2 - x + 1}{x^2 + 1}$ .

Answer:  A 0  B  $-\frac{3}{2}$   C -e  D Does not exist  E 1  F  $\pi$  → **E**

Family name:

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For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[3]{a^3b^3}\sqrt[4]{a^2b^3c^3}}{(a^2b^3)\sqrt[3]{bc^4}}$ .

- Answer:  A  $\frac{a^{11/2}}{b^{11/12}c^{7/4}}$      B  $\frac{1}{\sqrt{ab^{19/12}c^{7/12}}}$      C  $\frac{c^{3/5}}{\sqrt[9]{ab^{53/30}}}$      D  $\frac{1}{a^{5/2}b^{11/10}\sqrt{c}}$      E  $\frac{1}{a^{8/3}b^{13/6}\sqrt{c}}$

→ **B**

2) Compute all solutions of the system

$$\begin{cases} 4x - 4y + 2 = x + 2y \\ y - 3x = x - y. \end{cases}$$

- Answer:  A  $x = -\frac{4}{29}$  and  $y = -\frac{14}{29}$      B  $x = \frac{2}{9}$  and  $y = \frac{4}{9}$      C  $x = \frac{2}{11}$  and  $y = \frac{14}{11}$      D  $x = -\frac{8}{23}$  and  $y = \frac{2}{23}$      E  $x = \frac{8}{31}$  and  $y = -\frac{14}{31}$

→ **B**

3) Compute all solutions of the inequality  $2|x - 3| + x - 1 \leq x^2$ .

- Answer:  A  $x \leq 2$      B  $x \leq \frac{1}{2}(-1 - \sqrt{21})$  or  $x \geq \frac{1}{2}(\sqrt{21} - 1)$      C  $x \geq \frac{1}{3}$      D  $x \leq \frac{1}{6}(-5 - \sqrt{61})$  or  $x \geq \frac{1}{6}(\sqrt{61} - 5)$      E  $\frac{1}{2}(-1 - \sqrt{21}) \leq x \leq \frac{1}{2}(\sqrt{21} - 1)$

→ **B**

4) Compute all solutions of the system of inequalities

$$\begin{cases} x + 2 \leq -2x^2 - x \\ x + 1 > |1 - 2x|. \end{cases}$$

- Answer:  A No  $x$      B  $x > 1$  or  $x \leq 0$      C  $x > 4$      D  $-\frac{1}{4} < x \leq \frac{1}{2}(1 + \sqrt{5})$      E  $0 < x \leq \frac{1}{2}(\sqrt{5} - 1)$

→ **A**

5) Find the domain of definition of the expression:  $\log\left(\frac{(-2+x)(4+x)}{1+2x}\right)$ .

- Answer:  A  $-4 < x < -\frac{1}{2}$  or  $x > 2$      B  $x < -\frac{1}{2}$  or  $\frac{1}{2} < x < 3$      C  $-1 < x < -\frac{1}{2}$      D  $-4 < x < -\frac{3}{2}$  or  $x > 0$      E  $x < -2$  or  $-\frac{3}{2} < x < 0$

→ **A**

6) Find all  $x$  such that  $\frac{(-1+x)(3-3x)}{2+3x} < 0$ .

- Answer:  A  $x < -3$  or  $x > 0$      B  $x < -3$  or  $-1 < x < -\frac{1}{3}$      C  $x < -\frac{1}{2}$  or  $-\frac{1}{3} < x < 3$      D  $x < -\frac{5}{3}$  or  $-\frac{2}{3} < x < 1$      E  $-\frac{2}{3} < x < 1$  or  $x > 1$

→ **E**

7) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{e^{-2x}}{x^2} - \frac{e^{3x}}{x}$ .

- Answer:  A  $+\infty$      B 1     C  $e$      D  $-\infty$      E  $\pi$      F Does not exist

→ **A**

8) Compute the limit  $\lim_{x \rightarrow \frac{3}{5}-} \frac{e^{-1/x}}{5x-3}$ .

- Answer:  A  $-\pi$      B  $+\infty$      C Does not exist     D 2     E  $\pi$      F  $-\infty$

→ **F**

9) Compute the limit  $\lim_{x \rightarrow 0+} -\frac{3}{x^4} - x - 3 \log(x)$ .

- Answer:  A 2     B  $+\infty$      C  $e$      D Does not exist     E  $-\infty$      F  $-1$

→ **E**

10) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{2x^3 + 2x^2 + 1}{x^2 - 2x^3}$ .

- Answer:  A  $\frac{1}{2}$      B 1     C  $-\frac{1}{2}$      D Does not exist     E  $-1$      F  $\pi$

→ **E**

Family name:

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For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[5]{a^7 b^5} \sqrt[6]{a^2 b^3 c^4}}{(a^3 b^3) \sqrt[3]{b c^6}}$ .

- Answer:  A  $\frac{12\sqrt{c}}{a^{5/6}b^{17/6}}$      B  $\frac{c^{3/2}}{\sqrt[3]{ab^{19/12}}}$      C  $\frac{a^{23/3}\sqrt[6]{b}}{\sqrt[6]{c}}$      D  $\frac{a^{7/5}c^{4/3}}{b^{3/2}}$      E  $\frac{1}{a^{19/15}b^{11/6}c^{4/3}}$

→ E

2) Compute all solutions of the system

$$\begin{cases} x + 2y + 2 = y - 2x \\ y - 3x = 4x - 2y. \end{cases}$$

- Answer:  A  $x = -\frac{2}{25}$  and  $y = -\frac{14}{25}$      B  $x = -\frac{6}{35}$  and  $y = \frac{2}{5}$      C  $x = -\frac{3}{8}$  and  $y = -\frac{7}{8}$      D  $x = \frac{3}{5}$  and  $y = -\frac{4}{5}$      E  $x = \frac{2}{3}$  and  $y = -\frac{14}{9}$

→ C

3) Compute all solutions of the inequality  $-3|x - 1| - x - 1 > x^2$ .

- Answer:  A  $-1$      B  $x < \frac{1}{3}$  or  $x > 3$      C  $x < \frac{1}{2}(1 - \sqrt{5})$  or  $x > \frac{1}{2}(1 + \sqrt{5})$      D  $x < -3$  or  $x > 1$      E No  $x$

→ E

4) Compute all solutions of the system of inequalities

$$\begin{cases} |x + 1| + 2x \leq 1 \\ x^2 - 2x + 2 > x + 2. \end{cases}$$

- Answer:  A  $0 < x < 4$      B  $x > 0$      C  $-4 \leq x < -1$      D  $x < 0$      E  $x \geq \frac{5}{3}$

→ D

5) Find the domain of definition of the expression:  $\log\left(\frac{(-1+2x)(2+x)}{1+2x}\right)$ .

- Answer:  A  $-2 < x < -\frac{1}{2}$  or  $x > \frac{1}{2}$      B  $-4 < x < \frac{1}{2}$  or  $x > 3$      C  $\frac{1}{4} < x < \frac{1}{2}$  or  $x > 4$      D  $x < -4$  or  $-3 < x < 0$      E  $x < -\frac{1}{4}$  or  $x > 2$

→ A

6) Find all  $x$  such that  $\frac{(1+x)(2-3x)}{1+3x} < 0$ .

- Answer:  A  $-\frac{1}{2} < x < 0$  or  $x > 1$      B  $x < -1$  or  $-\frac{1}{3} < x < 3$      C  $-1 < x < -\frac{1}{3}$  or  $x > \frac{2}{3}$      D  $\frac{2}{3} < x < 1$      E  $-2 < x < -1$  or  $x > \frac{2}{3}$

→ C

7) Compute the limit  $\lim_{x \rightarrow +\infty} e^{-x} - \frac{e^{2x}}{x^3}$ .

- Answer:  A  $-\infty$      B  $2$      C  $-e$      D  $1$      E  $\pi$      F Does not exist

→ A

8) Compute the limit  $\lim_{x \rightarrow 0^+} \frac{e^{-2/x}(-x-2)}{x+2}$ .

- Answer:  A Does not exist     B 0     C  $-\pi$      D 2     E  $-1$      F  $e$

→ B

9) Compute the limit  $\lim_{x \rightarrow 0^+} -3x^2 - x + \log(x)$ .

- Answer:  A 1     B Does not exist     C  $\pi$      D 2     E  $e$      F  $-\infty$

→ F

10) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{3x^2 + x + 1}{-2x^3 + x^2 + 1}$ .

- Answer:  A Does not exist     B 0     C  $-1$      D  $\pi$      E 3     F  $\frac{3}{2}$

→ B

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For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[3]{a^3b^3}\sqrt{a^2b^2c^2}}{(a^4b^3)\sqrt[4]{bc^4}}$ .

Answer:  A  $\frac{a^{4/3}b^{7/15}}{c^{7/10}}$

B  $\frac{1}{\sqrt{ab^2c^{13/12}}}$

C  $\frac{1}{a^2b^{5/4}}$

D  $\frac{a^{2/3}}{\sqrt[6]{c}}$

E  $\frac{\sqrt{c}}{a^{2/5}b^{7/4}}$

→ **C**

2) Compute all solutions of the system

$$\begin{cases} 4x + 2y - 2 = x + y \\ -3x - 2y = 4x + y. \end{cases}$$

Answer:  A  $x = 3$  and  $y = -7$      B  $x = \frac{2}{7}$  and  $y = 1$      C  $x = -\frac{4}{21}$  and  $y = \frac{2}{7}$      D  $x = -\frac{4}{9}$  and  $y = -\frac{2}{9}$   
 E  $x = \frac{1}{3}$  and  $y = \frac{7}{9}$

→ **A**

3) Compute all solutions of the inequality  $-2x^2 + |-x + 2| \geq -3x - 4$ .

Answer:  A  $x \leq 0$  or  $x \geq 1$      B  $x \leq \frac{1}{4}(-1 - \sqrt{17})$  or  $x \geq -\frac{1}{2}$      C  $\frac{1}{2}(1 - \sqrt{13}) \leq x \leq 1 + \sqrt{2}$      D  $-1 \leq x \leq 1 + \sqrt{3}$   
 E  $x \leq 6$

→ **C**

4) Compute all solutions of the system of inequalities

$$\begin{cases} |x+1| + 2x \leq 1 \\ x^2 + x + 2 > 2 - 3x. \end{cases}$$

Answer:  A  $x > 3$      B  $x < -4$      C  $x > 0$      D  $0 < x < 1$      E  $x \leq -5$

→ **B**

5) Find the domain of definition of the expression:  $\sqrt{\frac{(1-x)(3-3x)}{1+3x}}$ .

Answer:  A  $x < -2$  or  $-\frac{3}{2} \leq x \leq 4$      B  $-2 \leq x < 2$  or  $x \geq 4$      C  $x > -\frac{1}{3}$      D  $-\frac{1}{3} \leq x < \frac{1}{3}$  or  $x \geq \frac{4}{3}$   
 E  $-2 < x \leq 2$  or  $x \geq 3$

→ **C**

6) Find all  $x$  such that  $\frac{(3-x)(2-3x)}{3x} \geq 0$ .

Answer:  A  $-3 \leq x < \frac{2}{3}$  or  $x \geq 2$      B  $-3 \leq x \leq -\frac{3}{2}$  or  $x > 0$      C  $x \leq -\frac{1}{2}$  or  $0 < x \leq \frac{2}{3}$   
 D  $\frac{1}{2} \leq x < \frac{2}{3}$  or  $x \geq 4$      E  $0 < x \leq \frac{2}{3}$  or  $x \geq 3$

→ **E**

7) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{e^{-3x}}{x} - e^{3x}x$ .

Answer:  A  $e$      B  $-\infty$      C  $2$      D  $-1$      E Does not exist     F  $0$

→ **B**

8) Compute the limit  $\lim_{x \rightarrow 0^-} \frac{e^{2/x}(2x-2)}{3x-1}$ .

Answer:  A  $-\pi$      B  $0$      C  $1$      D  $2$      E Does not exist     F  $-e$

→ **B**

9) Compute the limit  $\lim_{x \rightarrow 0^+} -x^2 + x - \log(x)$ .

Answer:  A  $1$      B  $+\infty$      C  $-1$      D Does not exist     E  $-\infty$      F  $0$

→ **B**

10) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{-4x^3 + 2x^2 + 1}{x^2 - 4x^3}$ .

Answer:  A  $-1$      B  $1$      C Does not exist     D  $+\infty$      E  $2$      F  $-e$

→ **B**

**30**

Family name:

First name:

Matr.no.:

For each question, choose ONE answer and write ONLY the letter of that answer at the end of the arrow

1) Simplify the following expression:  $\frac{\sqrt[5]{a^7b^5}\sqrt{a^2b^4c^3}}{(a^3b^2)\sqrt[3]{bc^6}}$ .

- Answer:  A  $\frac{a^{5/6}}{b^{13/30}\sqrt[5]{c}}$      B  $\frac{a^{19/3}}{b^{5/2}c^{31/30}}$      C  $\frac{b^{2/3}}{a^{3/5}\sqrt{c}}$      D  $\frac{1}{\sqrt[3]{ab^{11/6}c^{3/2}}}$      E  $\frac{1}{a^{12/5}b^{8/15}\sqrt{c}}$

→ C

2) Compute all solutions of the system

$$\begin{cases} -2x + 2y - 2 = x + y \\ y - 3x = x + 2y. \end{cases}$$

- Answer:  A  $x = \frac{2}{11}$  and  $y = \frac{14}{33}$      B  $x = 2$  and  $y = 7$      C  $x = -\frac{2}{7}$  and  $y = \frac{8}{7}$      D  $x = \frac{2}{7}$  and  $y = -\frac{8}{7}$      E  $x = -\frac{2}{11}$  and  $y = \frac{8}{33}$

→ C

3) Compute all solutions of the inequality  $-2|x+1| + x - 1 > -2x^2$ .

- Answer:  A  $x < -\frac{1}{3}$      B  $x < \frac{1}{2}(5 - 3\sqrt{5})$  or  $x > \frac{1}{2}(5 + 3\sqrt{5})$      C  $x < -1$  or  $x > \frac{3}{2}$      D  $x < -1$  or  $x > \frac{1}{2}$      E  $-4 < x < \sqrt{3} - 1$

→ C

4) Compute all solutions of the system of inequalities

$$\begin{cases} |x+3| - 2x \leq 1 \\ x^2 + x + 2 > x + 2. \end{cases}$$

- Answer:  A  $x \geq 1$      B  $x > 0$      C  $x \geq 5$      D  $x \geq 2$      E  $-3 < x \leq -\frac{2}{3}$

→ D

5) Find the domain of definition of the expression:  $\log\left(\frac{(-3-x)(3+x)}{1-4x}\right)$ .

- Answer:  A  $x < -3$  or  $-1 < x < \frac{3}{2}$      B  $x > \frac{1}{4}$      C  $-\frac{1}{2} < x < 2$  or  $x > 4$      D 2     E  $\frac{1}{2} < x < 1$  or  $x > \frac{3}{2}$

→ B

6) Find all  $x$  such that  $\frac{-3-2x}{(5+x)(3x)} \leq 0$ .

- Answer:  A  $x < -1$  or  $x > \frac{1}{3}$      B  $x < -\frac{1}{3}$  or  $1 \leq x < 4$      C  $x \leq -\frac{3}{2}$  or  $\frac{1}{3} < x < 3$      D  $-\frac{3}{2} \leq x < -\frac{1}{3}$  or  $x > 5$      E  $-5 < x \leq -\frac{3}{2}$  or  $x > 0$

→ E

7) Compute the limit  $\lim_{x \rightarrow +\infty} e^{-2x} - \frac{e^{2x}}{x}$ .

- Answer:  A  $-\infty$      B  $+\infty$      C  $-\pi$      D Does not exist     E 2     F 0

→ A

8) Compute the limit  $\lim_{x \rightarrow 0+} \frac{e^{\frac{1}{x}}}{-x^2 - x + 1}$ .

- Answer:  A Does not exist     B  $\pi$      C  $\frac{1}{2}$      D  $-\pi$      E  $+\infty$      F 0

→ E

9) Compute the limit  $\lim_{x \rightarrow +\infty} \frac{5}{x^4} - 3x - \log(x)$ .

- Answer:  A  $\pi$      B 2     C  $+\infty$      D  $-\infty$      E  $-\pi$      F Does not exist

→ D

10) Compute the limit  $\lim_{x \rightarrow -\infty} \frac{2x^2 - 2x + 1}{4x^3 + x^2 + 1}$ .

- Answer:  A Does not exist     B 3     C 1     D  $-\infty$      E  $+\infty$      F 0

→ F

BONUS

## SOLUZIONI

↓Testo\Domanda→	1	2	3	4	5	6	7	8	9	10
I	E	D	B	B	A	E	A	F	B	D
II	C	A	E	E	D	E	B	D	F	F
III	E	A	C	D	A	E	E	C	C	B
IV	A	B	D	D	A	A	A	E	A	A
V	A	A	A	A	B	A	F	D	F	D
VI	D	C	C	B	E	E	A	F	A	E
VII	C	C	A	E	E	B	A	E	D	D
VIII	B	C	A	B	C	B	F	A	F	D
IX	C	E	C	A	E	E	E	E	F	D
X	B	A	D	B	A	A	F	C	C	F
XI	A	E	D	C	D	D	C	F	D	B
XII	D	E	E	E	B	C	E	C	E	B
XIII	C	D	E	A	D	B	F	C	D	F
XIV	A	E	C	C	A	A	A	E	C	F
XV	D	D	E	C	E	C	D	F	D	C
XVI	C	A	E	B	D	B	A	F	C	C
XVII	C	E	C	A	C	C	F	D	E	D
XVIII	E	E	E	A	B	E	D	B	E	E
XIX	B	C	B	A	B	E	D	D	D	B
XX	E	D	D	C	E	A	F	D	C	F
XXI	B	C	A	E	A	B	C	D	D	D
XXII	C	A	C	D	B	B	A	E	C	A
XXIII	E	A	D	E	E	B	C	F	B	A
XXIV	A	C	B	D	B	A	D	B	F	E
XXV	A	C	B	C	E	B	C	E	D	B
XXVI	A	C	B	A	A	B	C	B	E	E
XXVII	B	B	B	A	A	E	A	F	E	E
XXVIII	E	C	E	D	A	C	A	B	F	B
XXIX	C	A	C	B	C	E	B	B	B	B
XXX	C	C	C	D	B	E	A	E	D	F