

in this talk we will describe the construction of the so-called finite Verma modules for  $\mathbb{Z}$ -graded Lie superalgebras and study the finite Verma modules over the exceptional linearly compact Lie superalgebra  $E(5,10)$ . This is done through the classification of singular vectors. We will show that the corresponding morphisms of Verma modules can be arranged in an infinite number of bilateral infinite complexes which can be viewed as "exceptional" de Rham complexes for  $E(5,10)$ .